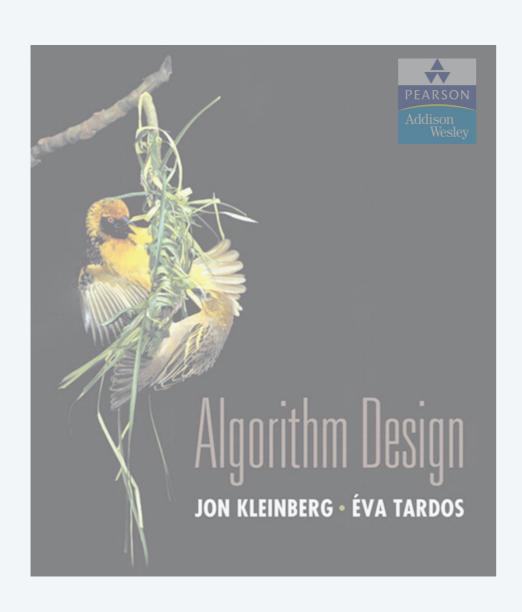


3. GPRAHS

- ▶ BFS demo
- ▶ DFS demo

Lecture slides by Kevin Wayne Copyright © 2005 Pearson-Addison Wesley

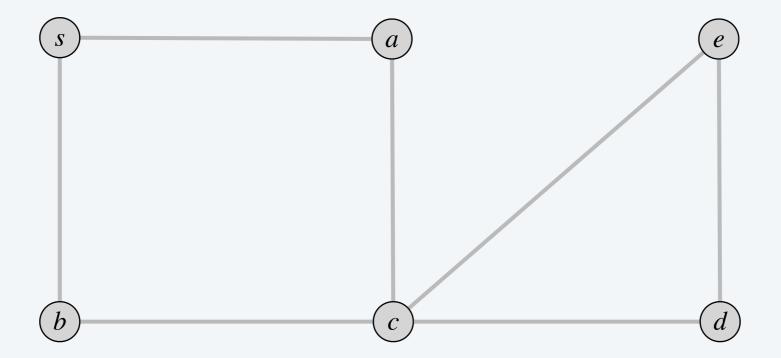
http://www.cs.princeton.edu/~wayne/kleinberg-tardos



3. GRAPHS

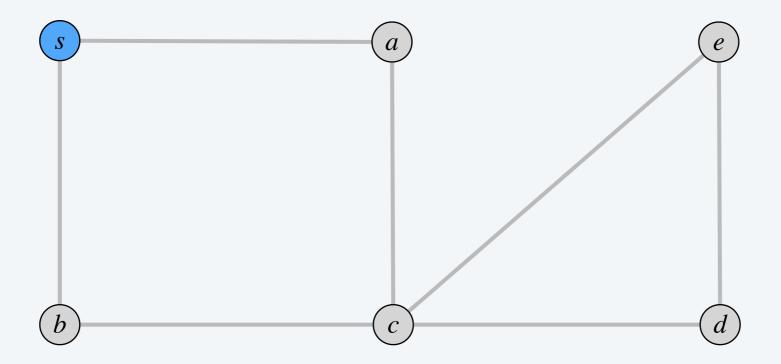
- ▶ BFS demo
- ▶ DFS demo

mark s as explored, all other vertices as unexplored Q := a queue, initialized with s while Q is not empty do remove the vertex from the front of Q, call it v for each edge (v, w) in v's adjacency list do if w is unexplored then mark w as explored add w to the end of Q



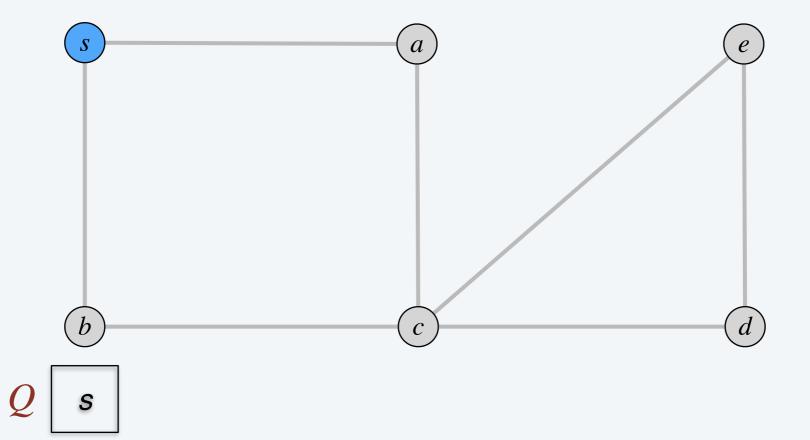
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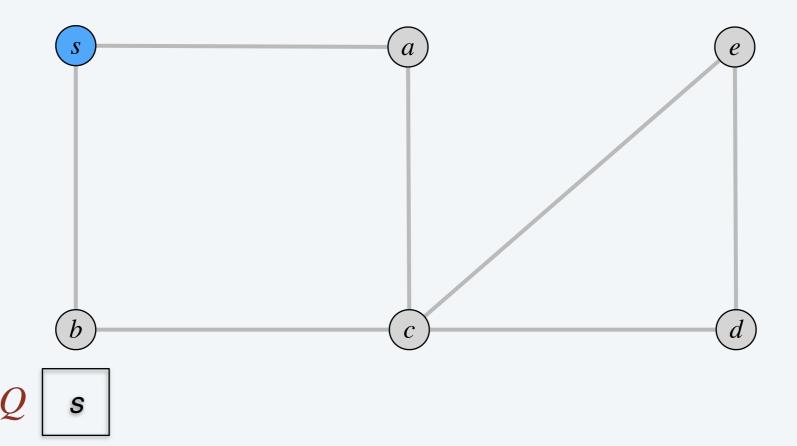
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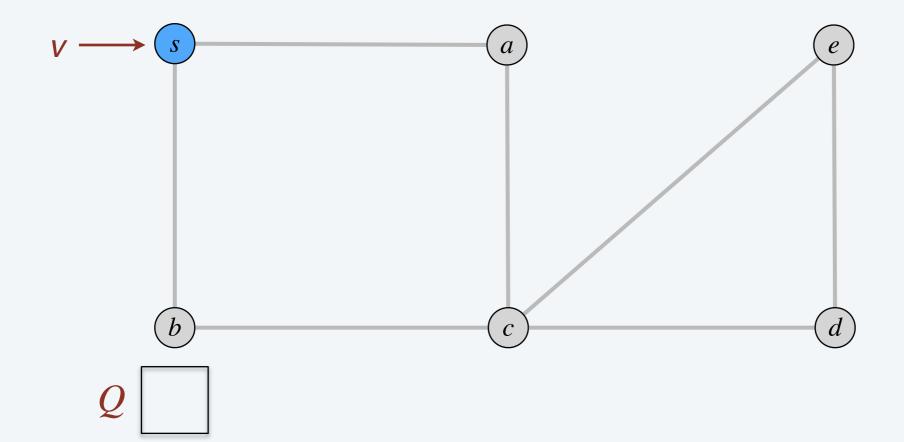
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remove the vertex from the front of Q, call it v

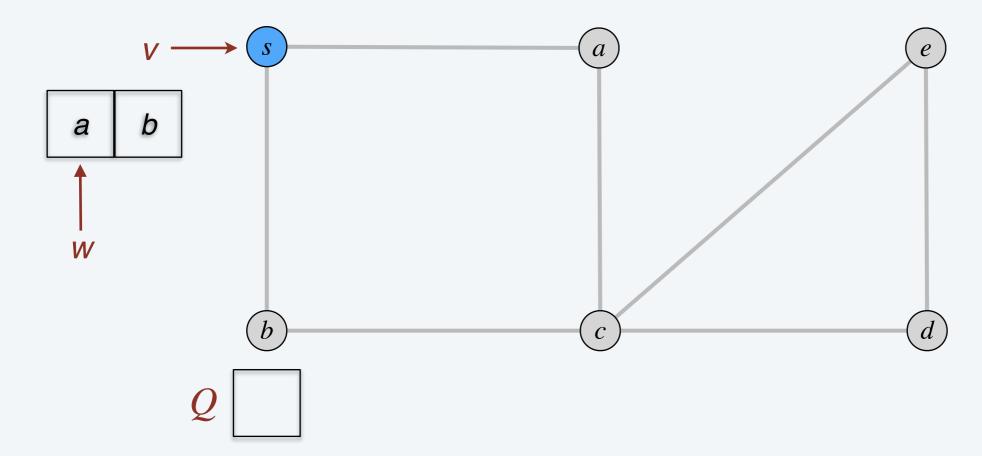
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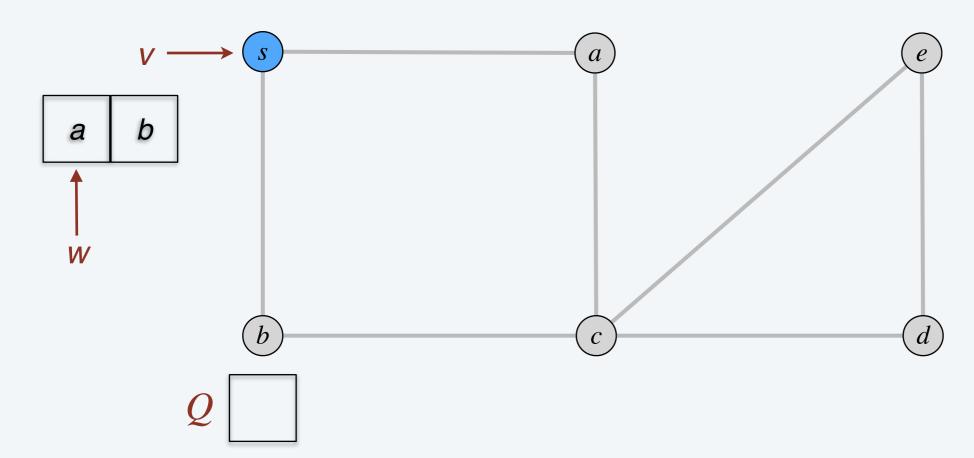
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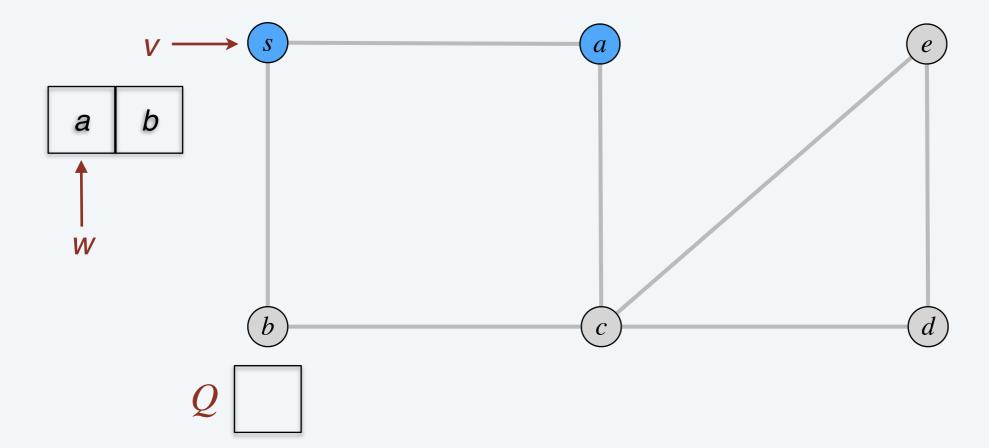
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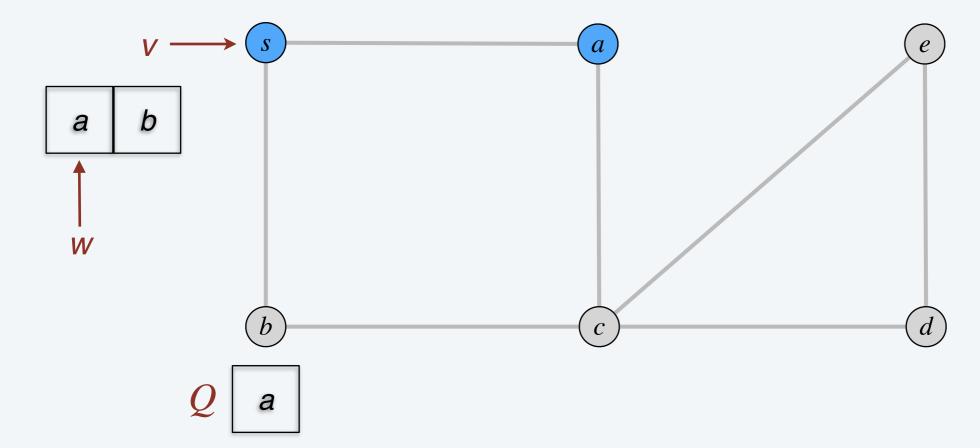


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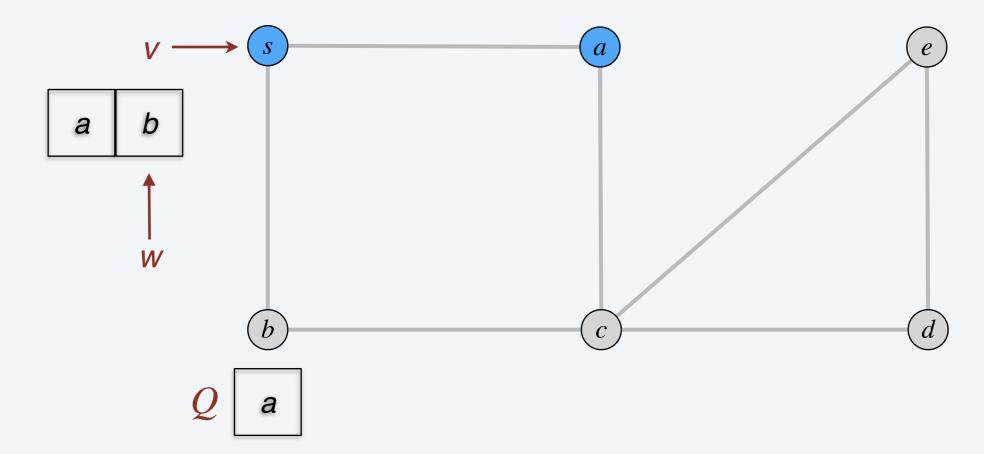
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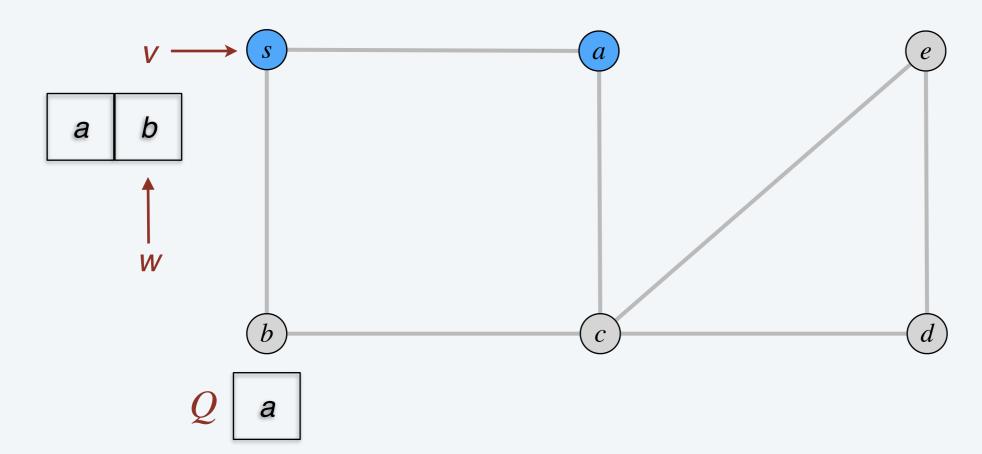
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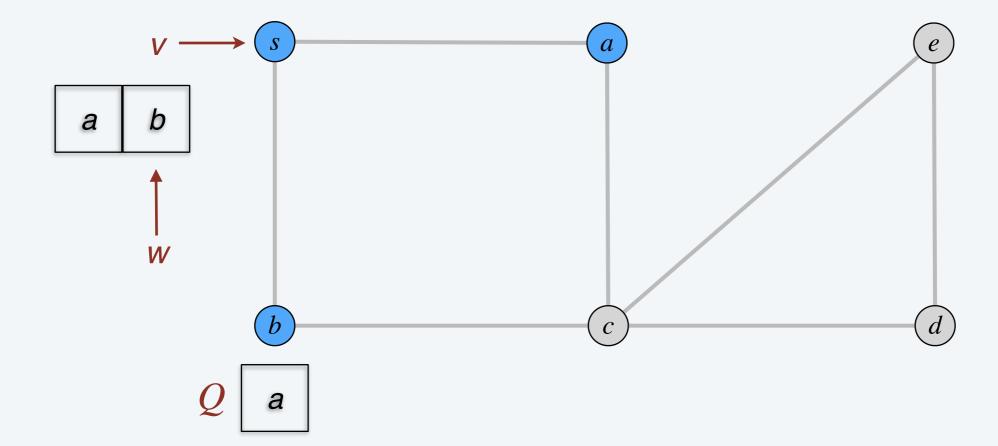
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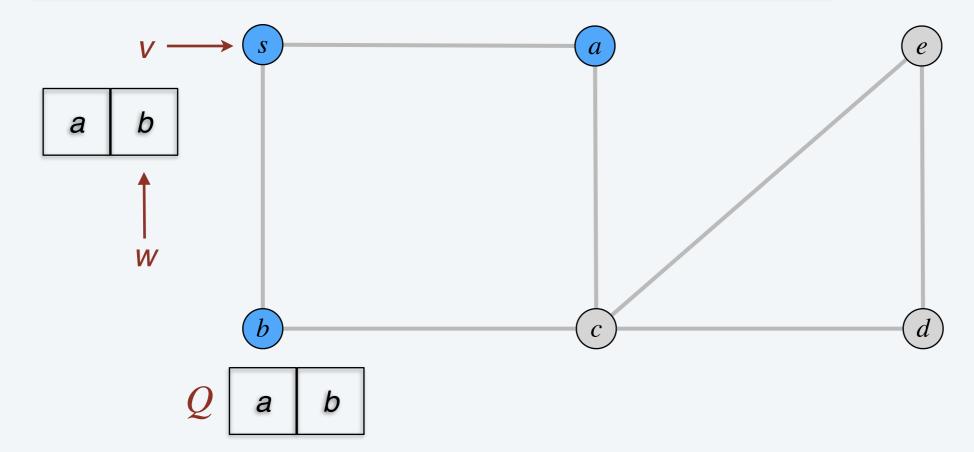


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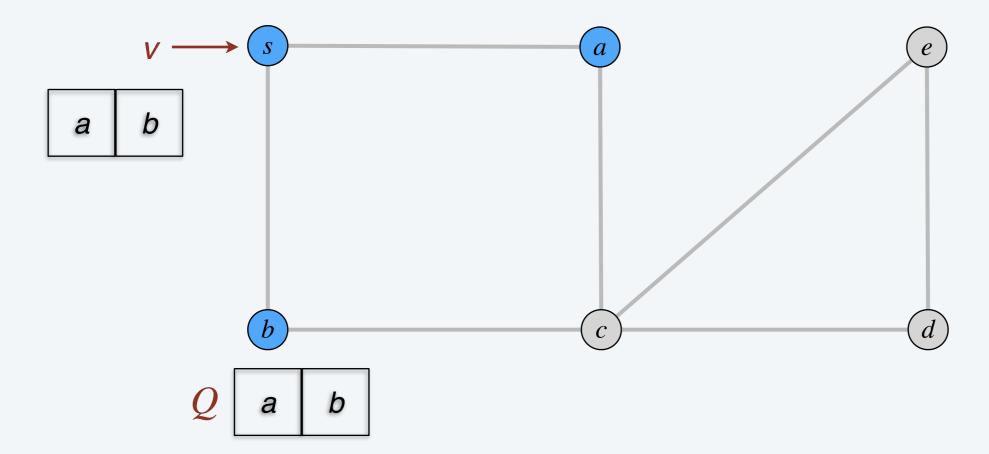
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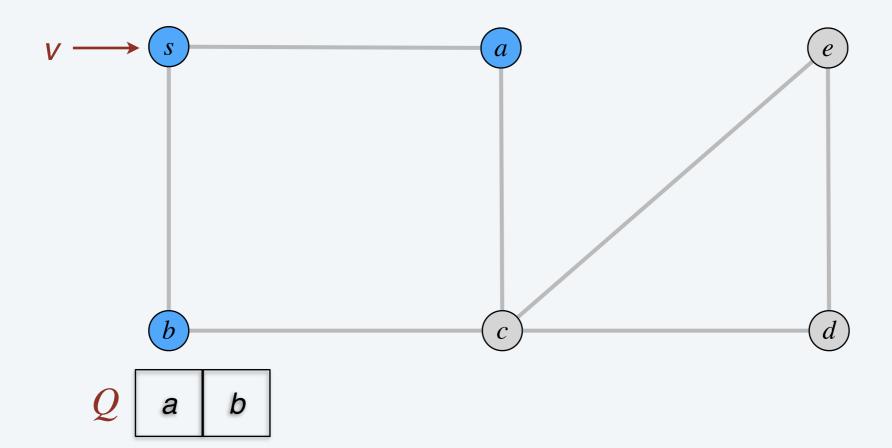
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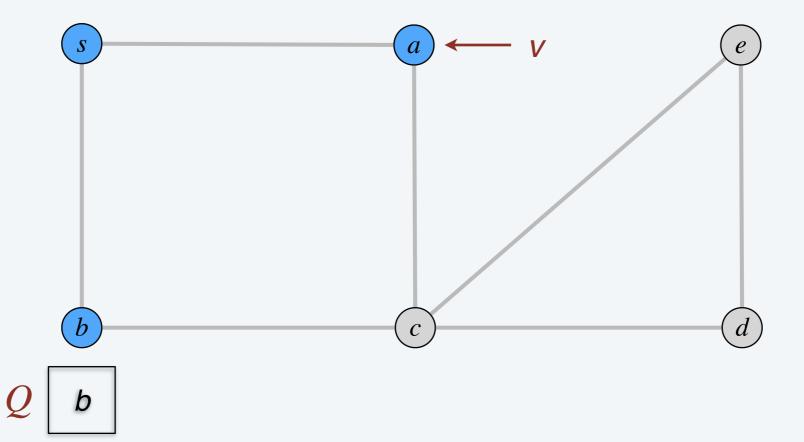
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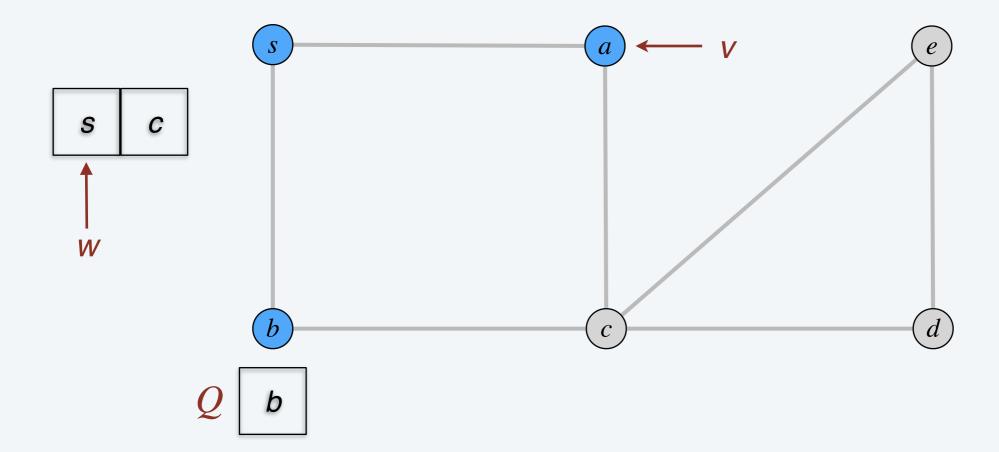
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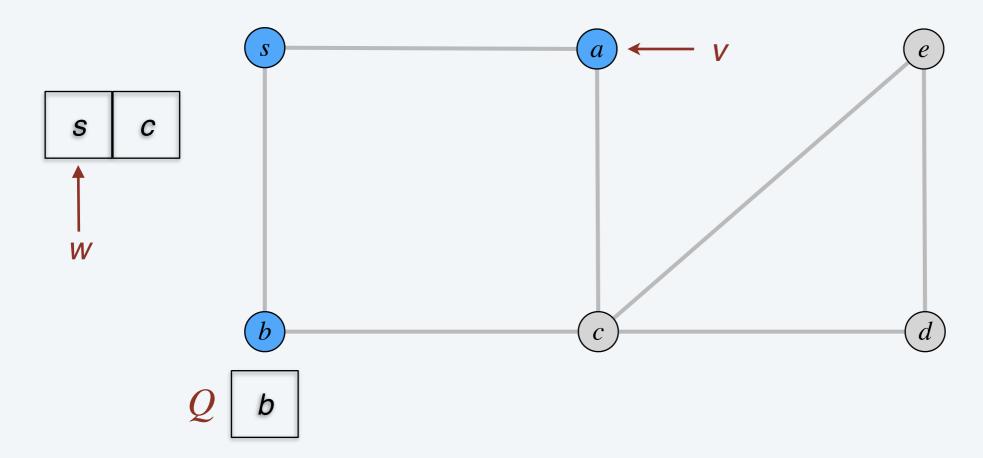
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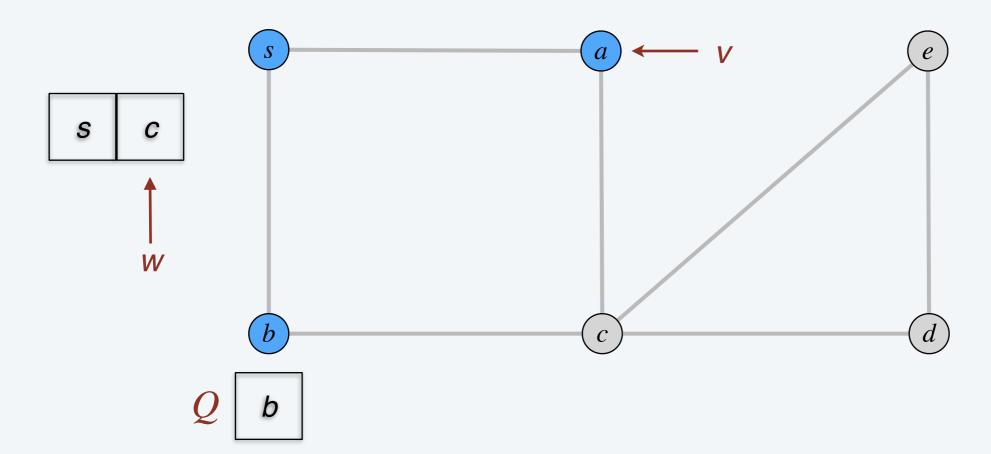
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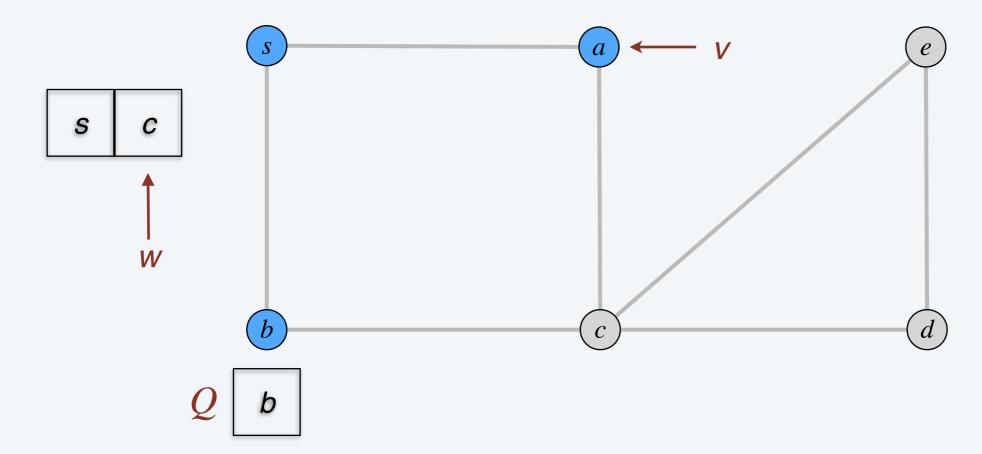
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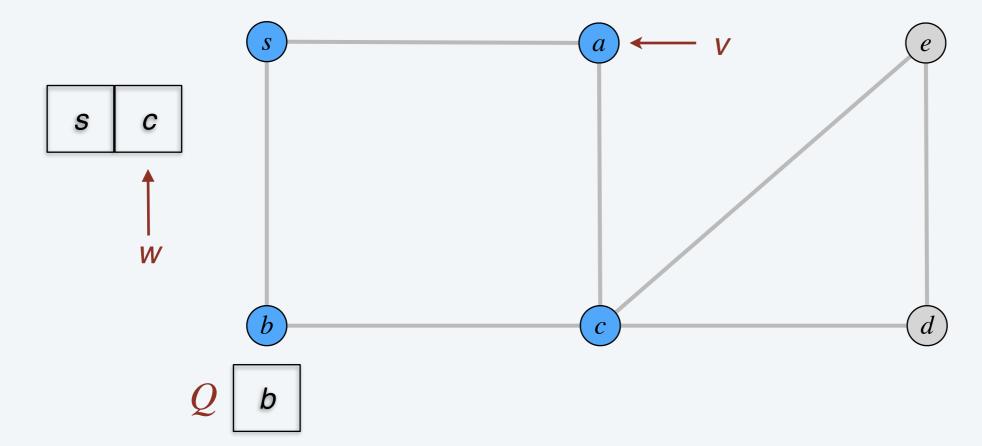
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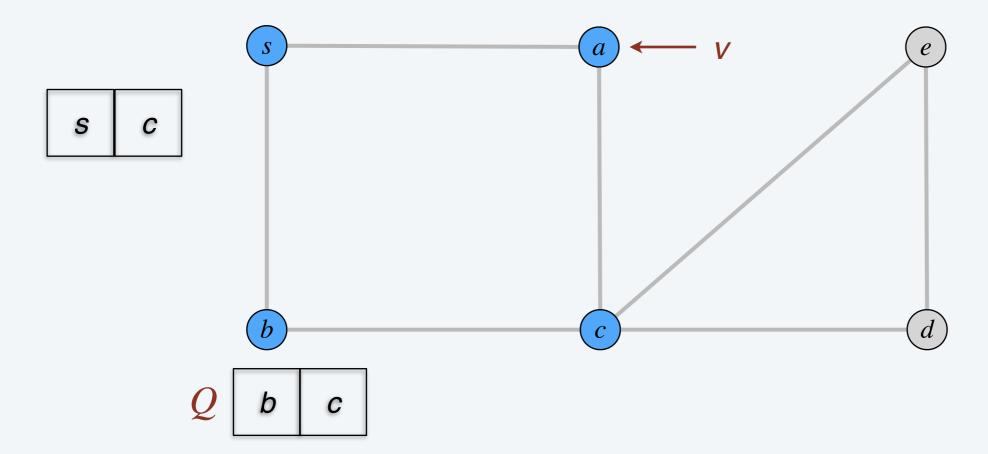


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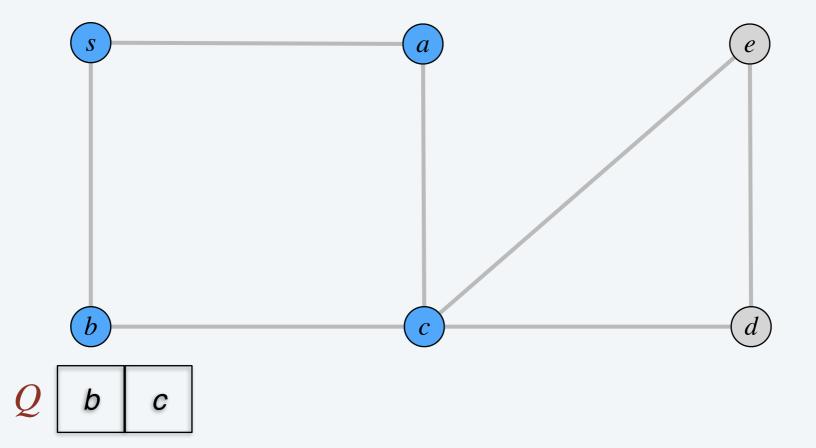
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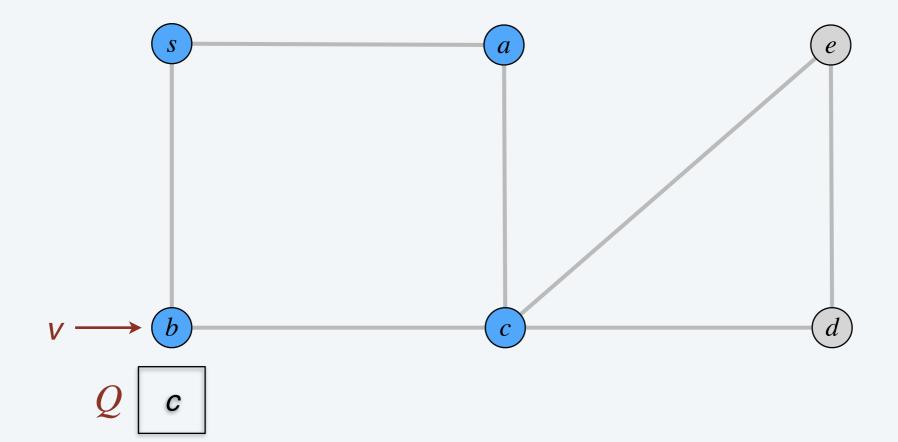
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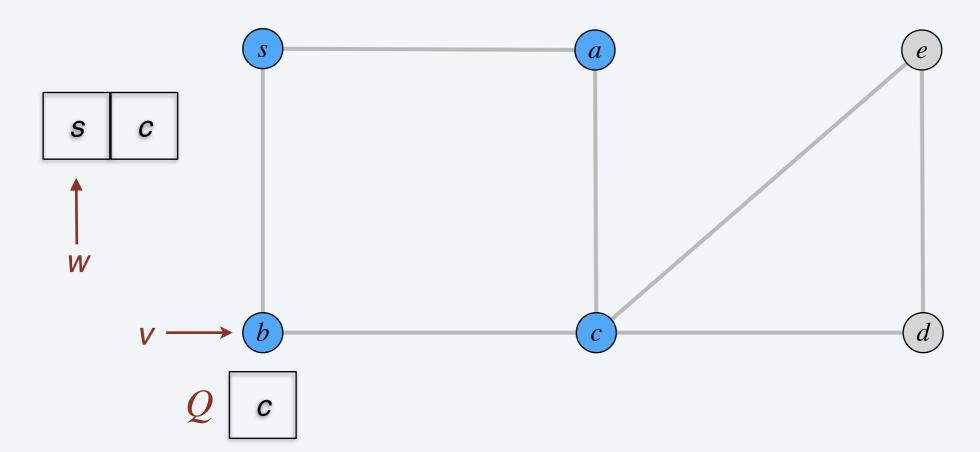
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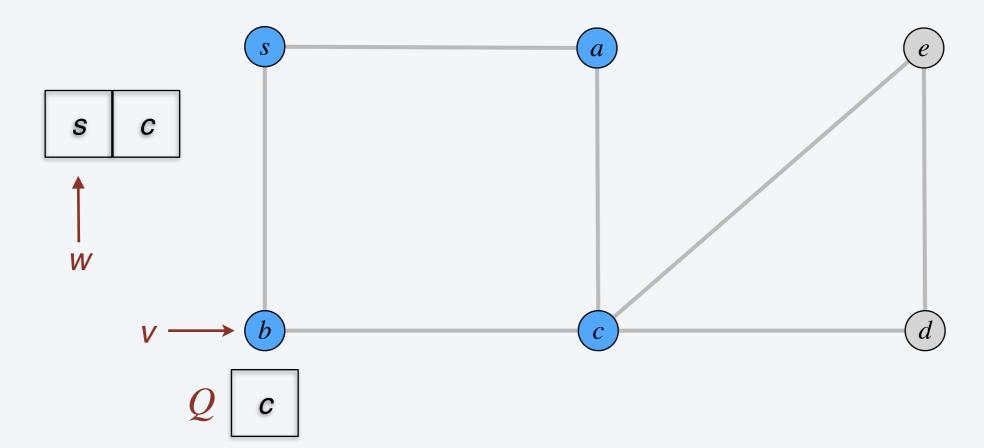
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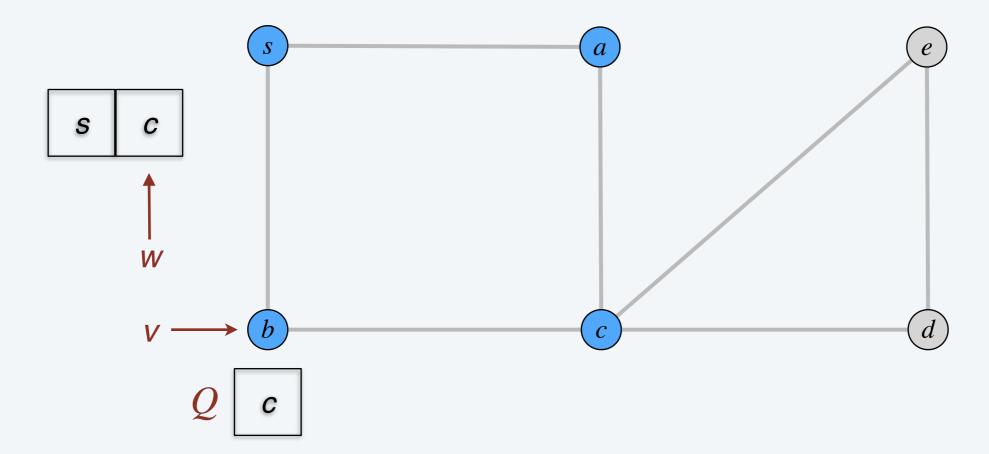
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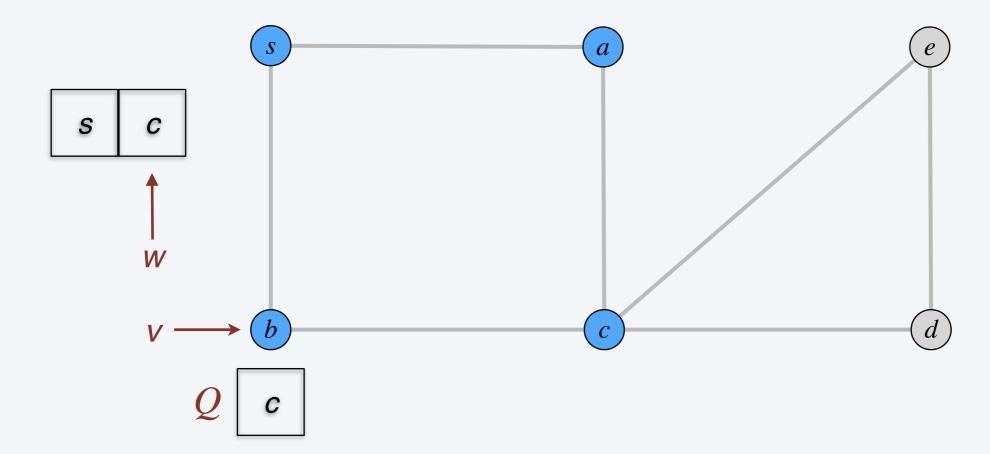
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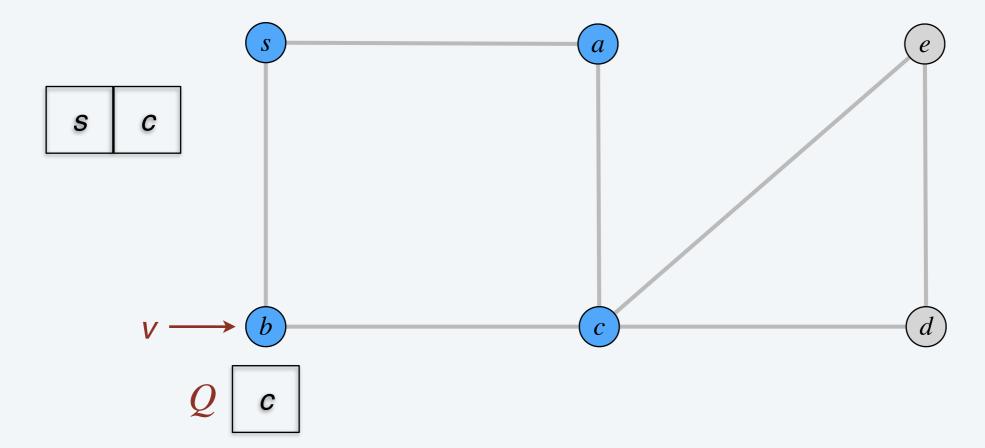
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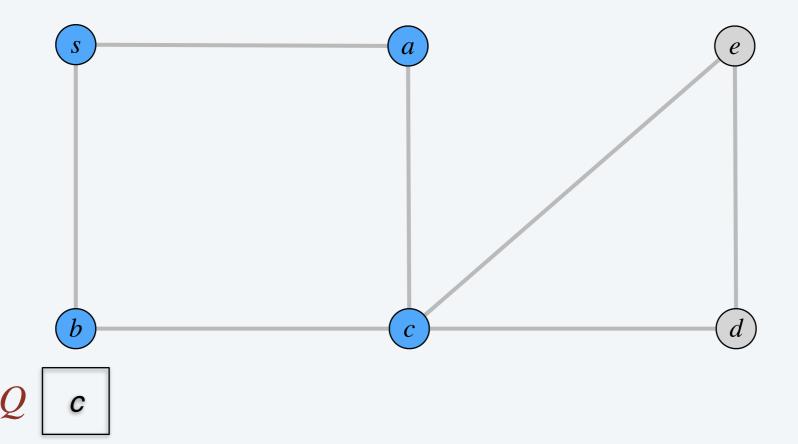
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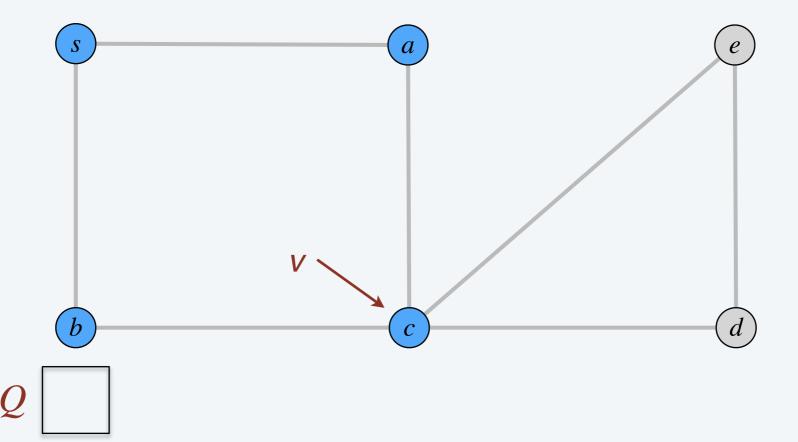
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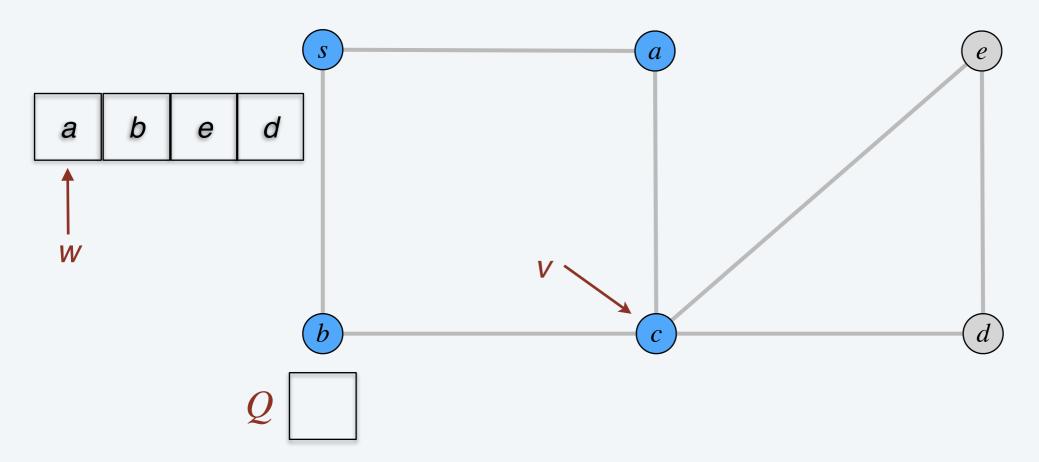
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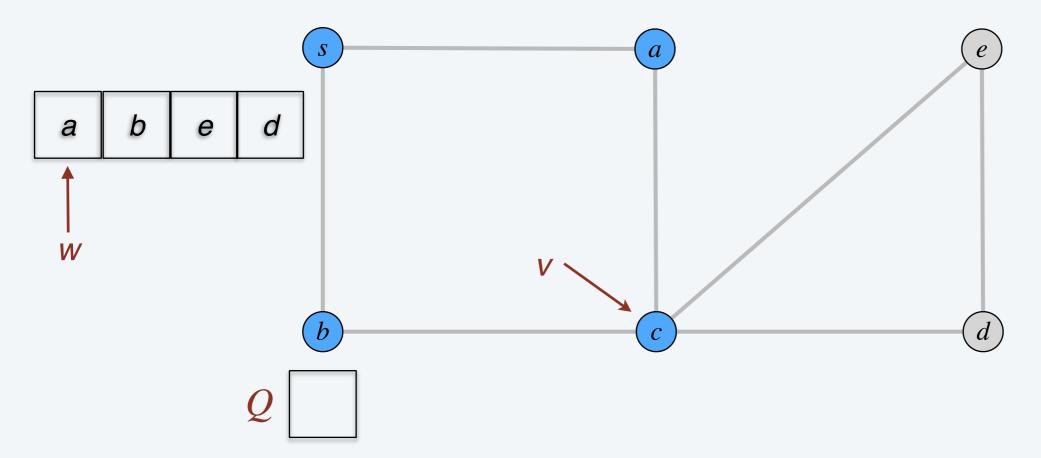
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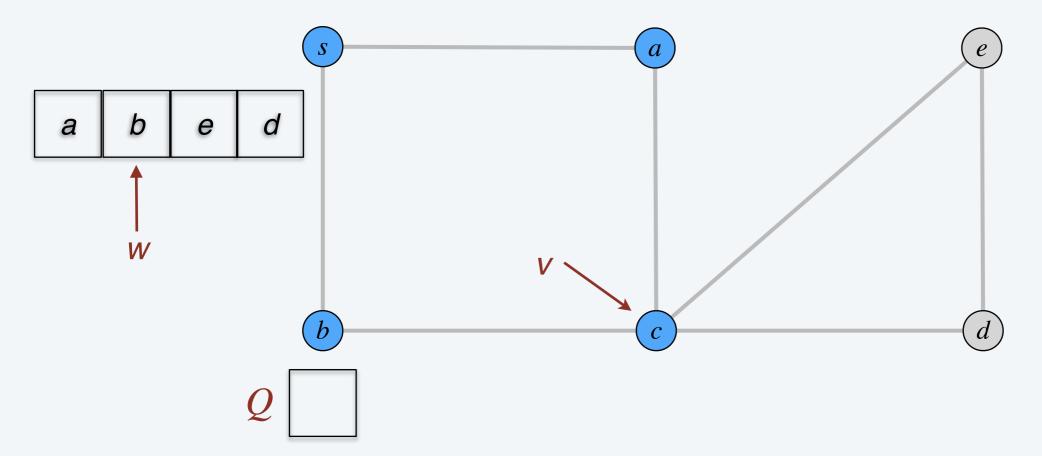
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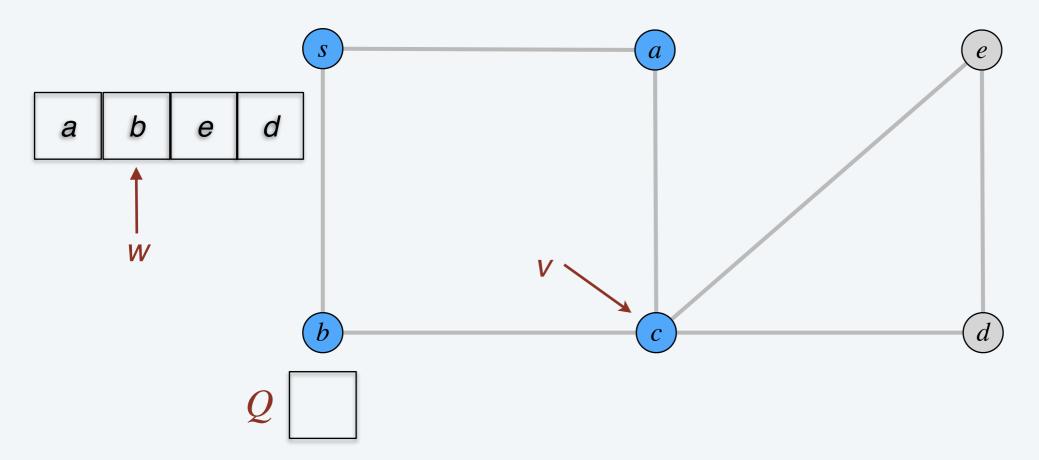
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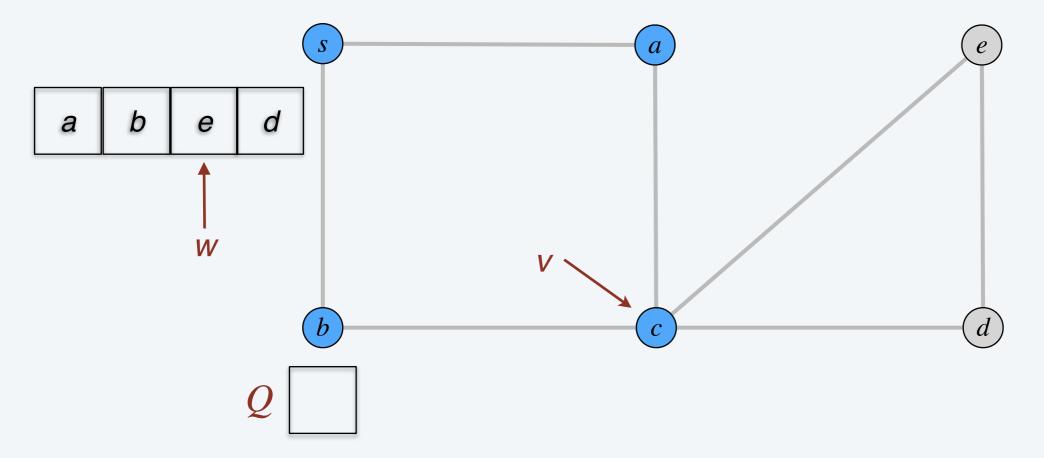
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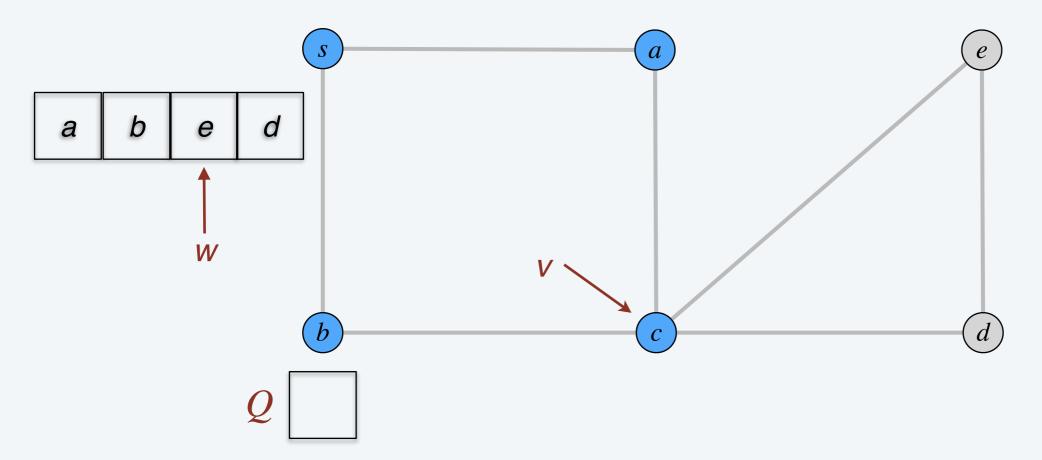
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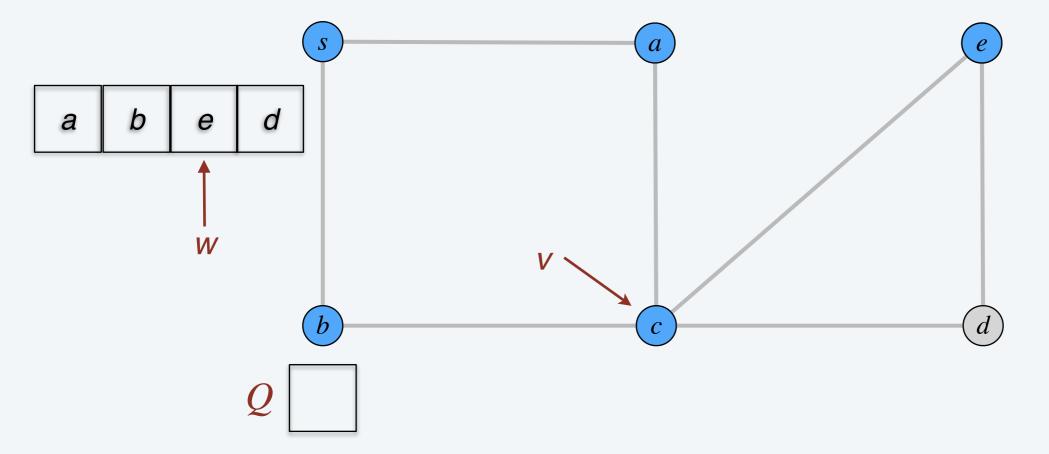
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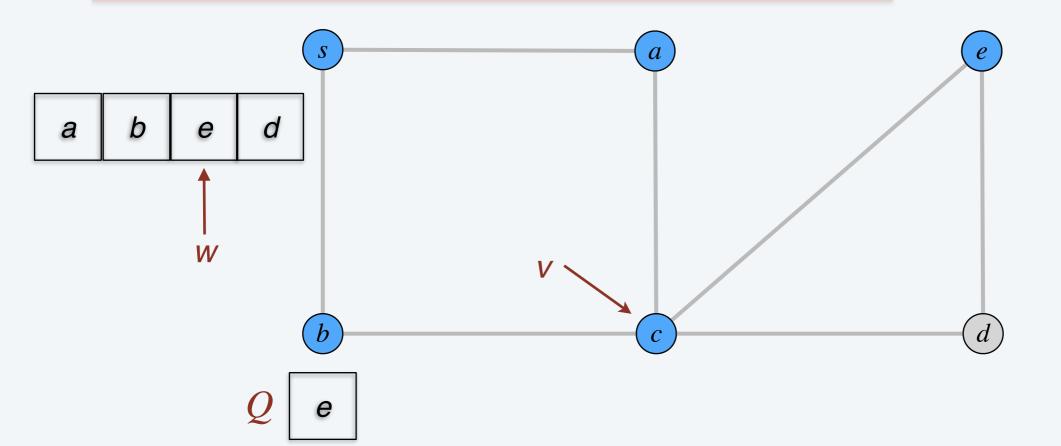
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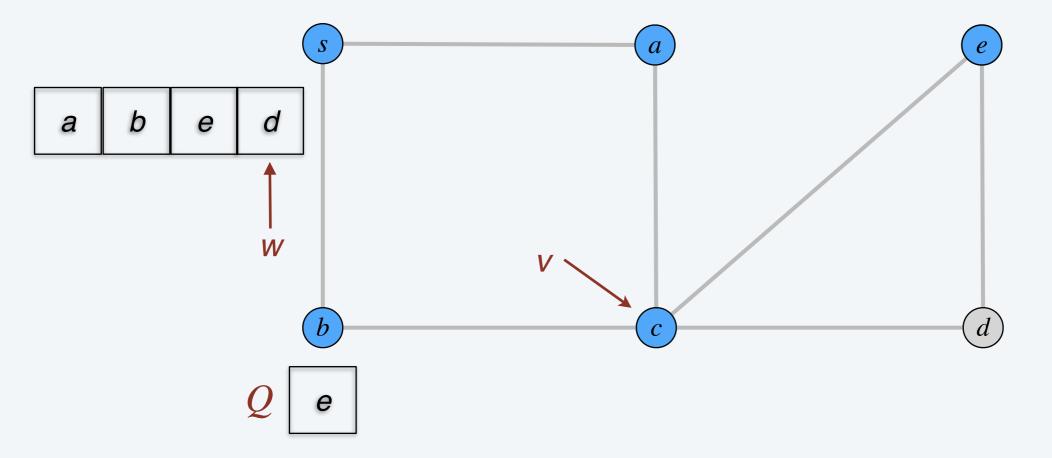
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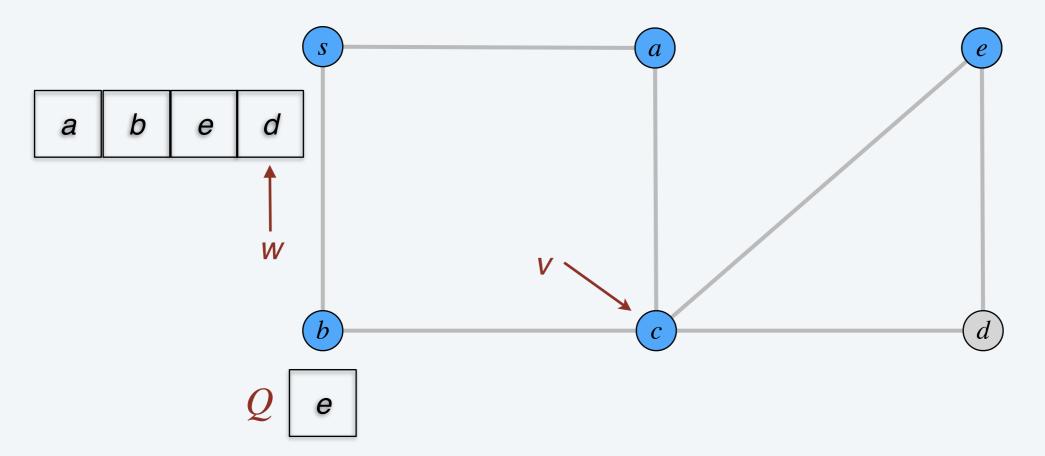
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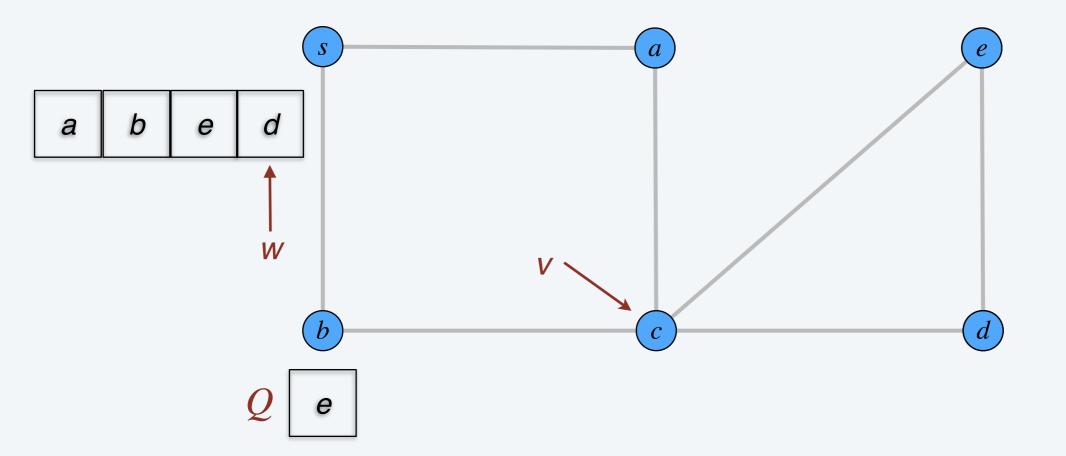
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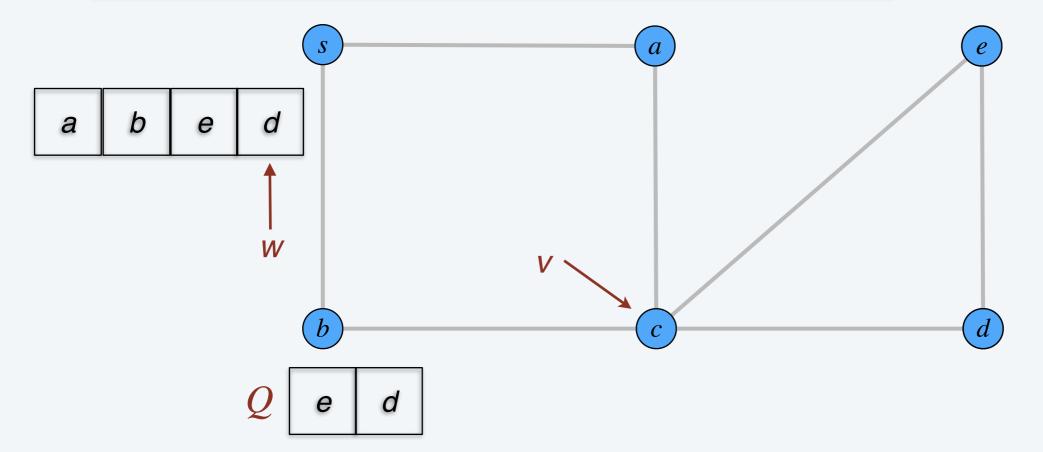
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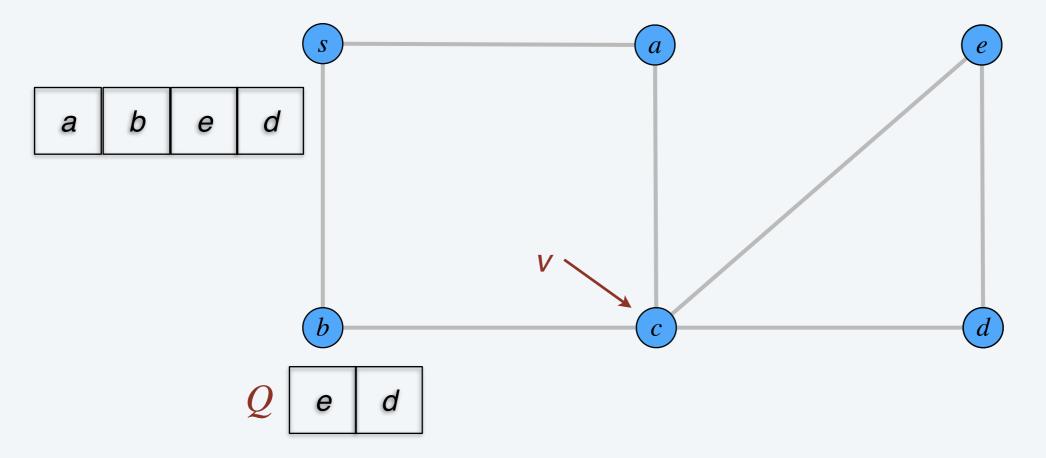
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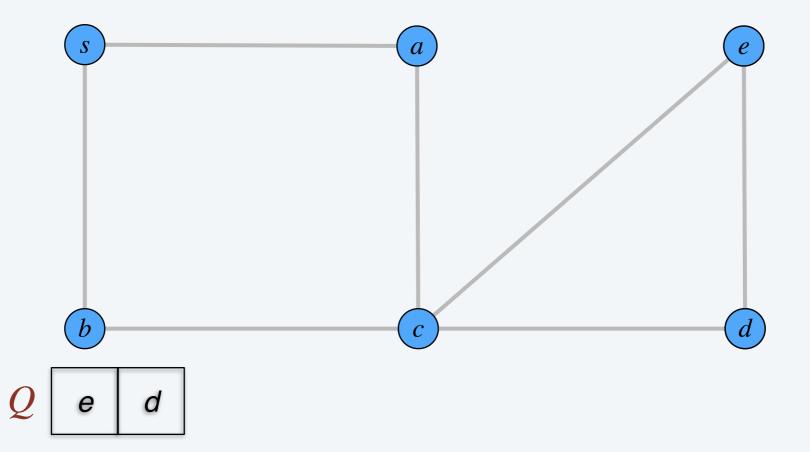
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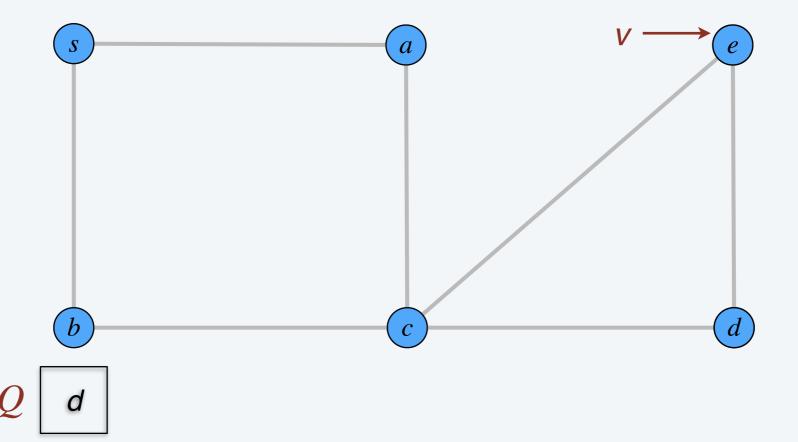
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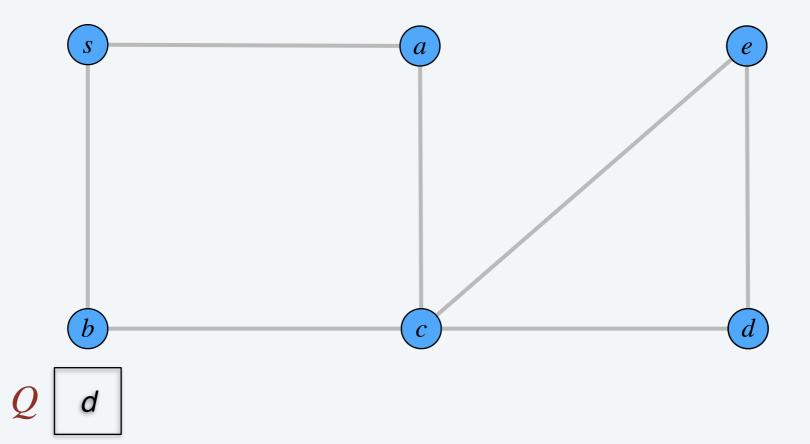
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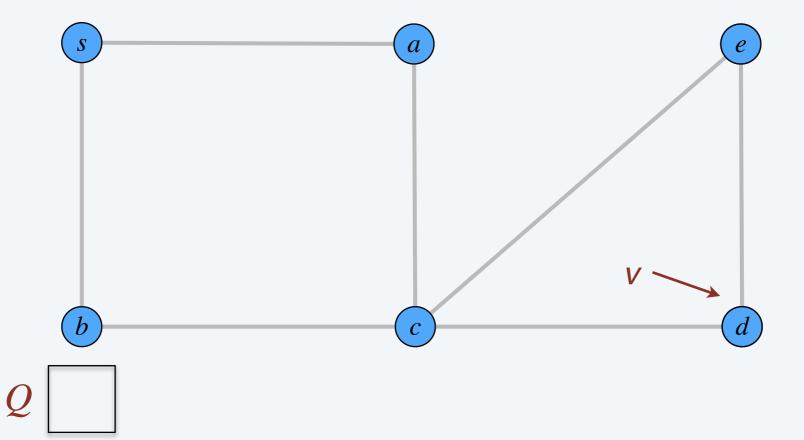
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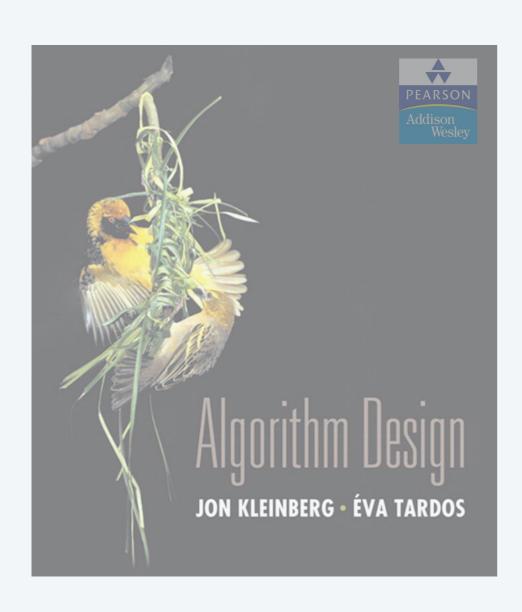


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3. GRAPHS

- ▶ BFS demo
- ▶ DFS demo

mark all vertices as unexplored

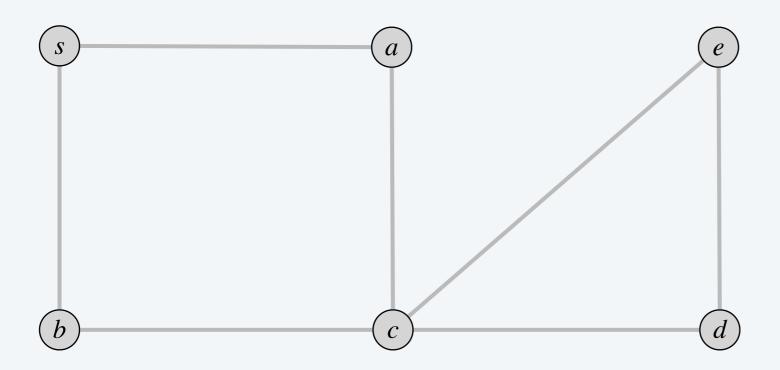
 $S \leftarrow$ a stack data structure, initialized with s

WHILE S is not empty

remove ("pop") the vertex v from the front of S

IF *v* is unexplored

mark v as explored



mark all vertices as unexplored

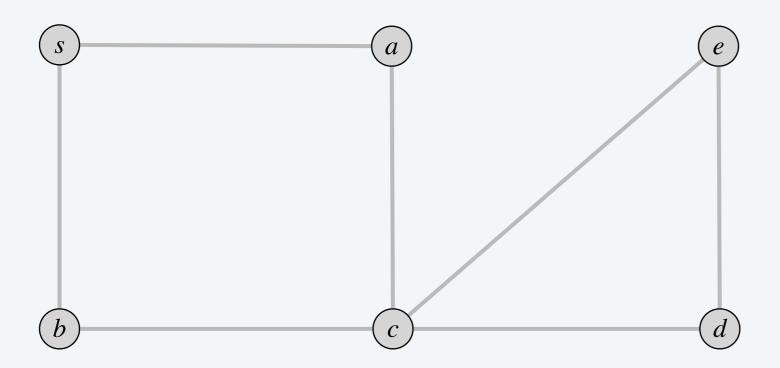
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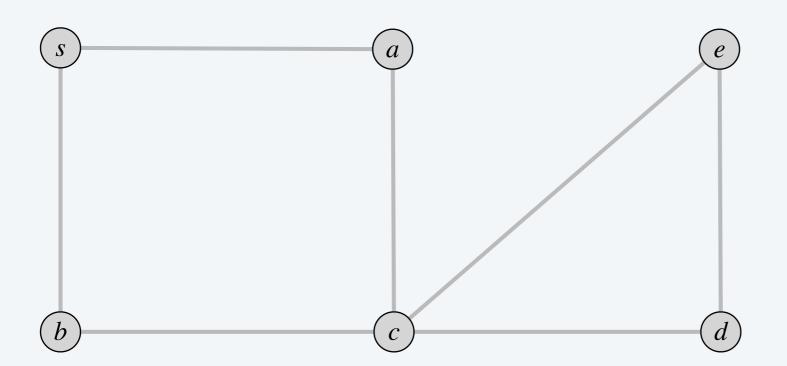
WHILE S is not empty

remove ("pop") the vertex v from the front of S

IF *v* is unexplored

mark v as explored

FOR each edge (*v*, *w*) in *v*'s adjacency-list add ("push") *w* to the front of *S*





S

mark all vertices as unexplored

 $S \leftarrow$ a stack data structure, initialized with s

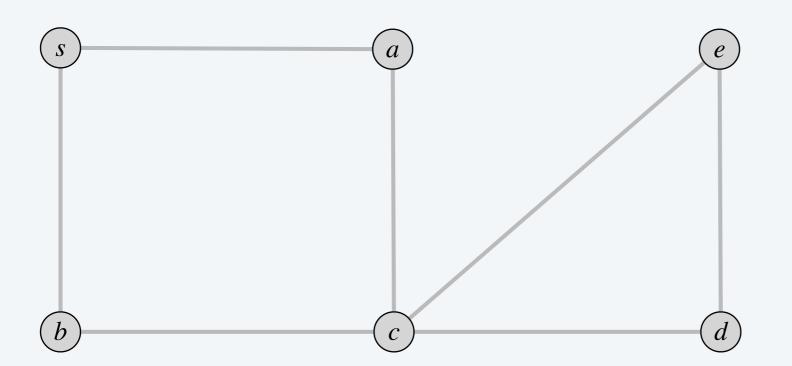
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remove ("pop") the vertex *v* from the front of *S*

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FOR each edge (*v*, *w*) in *v*'s adjacency-list add ("push") *w* to the front of *S*





S

mark all vertices as unexplored

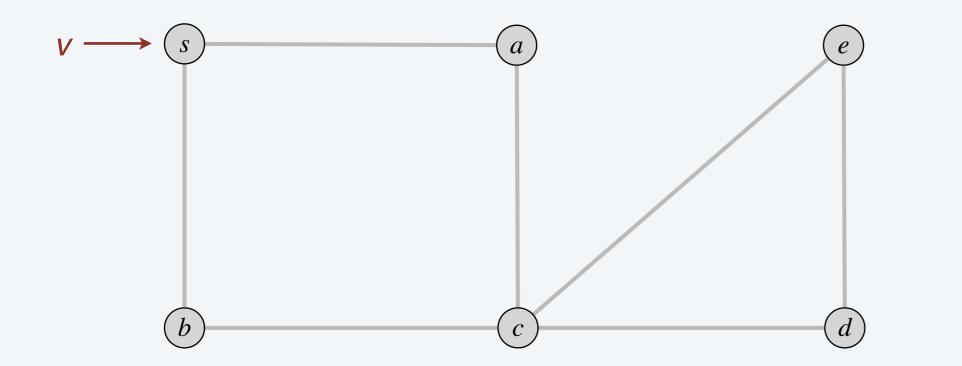
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mark all vertices as unexplored

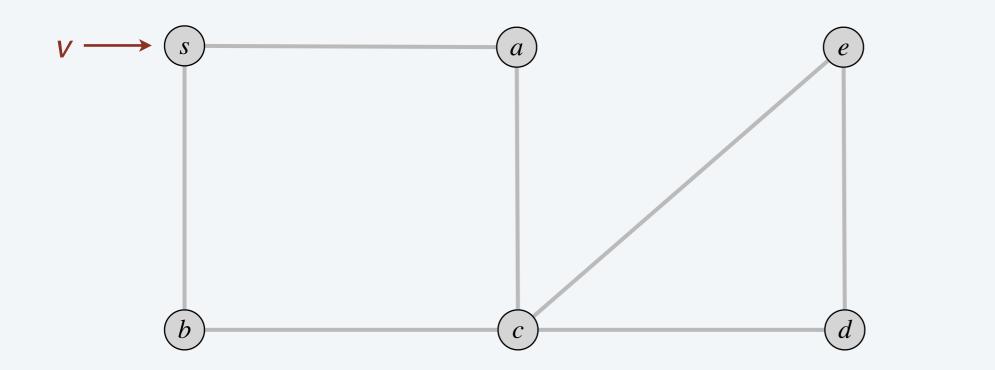
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mark all vertices as unexplored

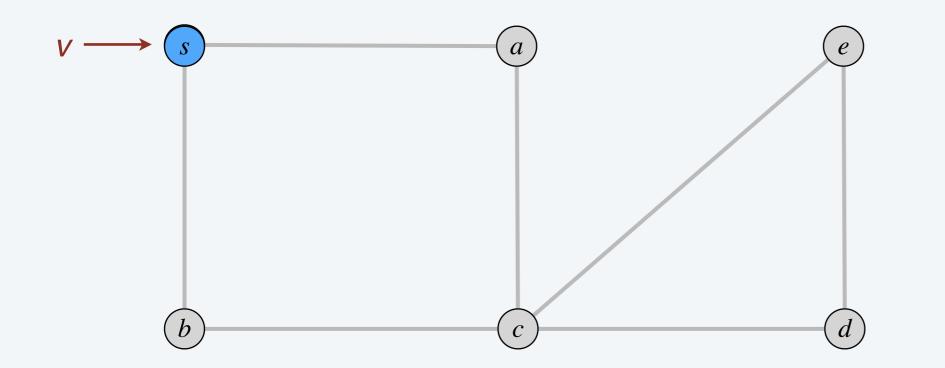
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WHILE S is not empty

remove ("pop") the vertex v from the front of S

IF *v* is unexplored

mark v as explored





mark all vertices as unexplored

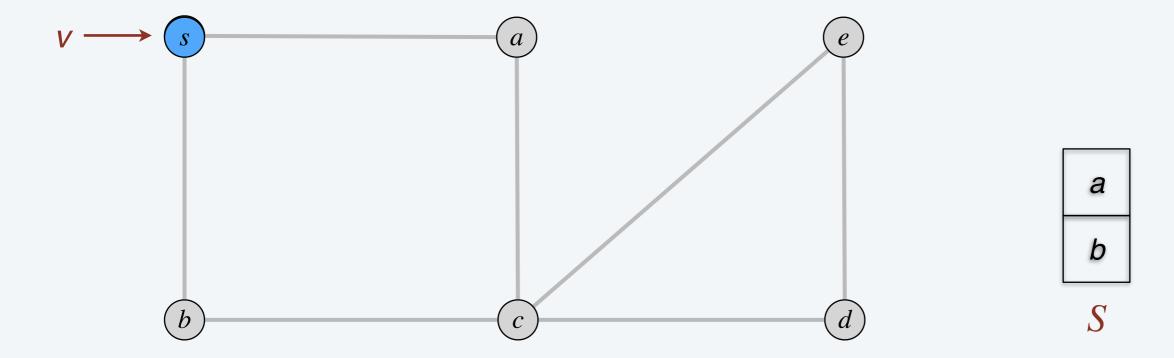
 $S \leftarrow$ a stack data structure, initialized with s

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mark all vertices as unexplored

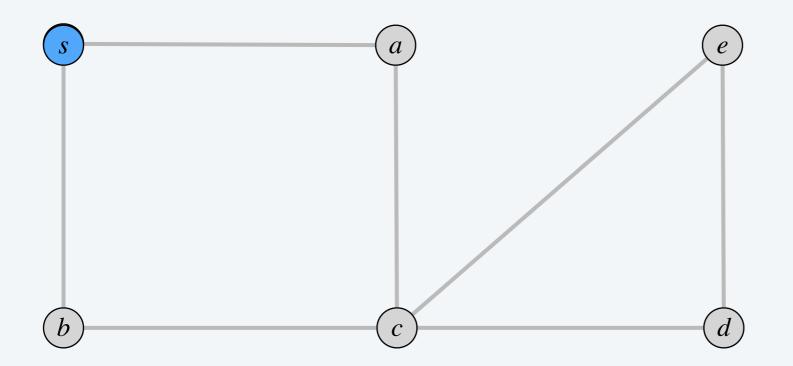
 $S \leftarrow$ a stack data structure, initialized with s

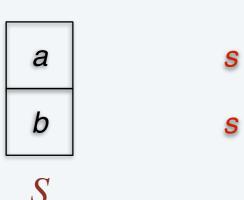
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mark v as explored





mark all vertices as unexplored

 $S \leftarrow$ a stack data structure, initialized with s

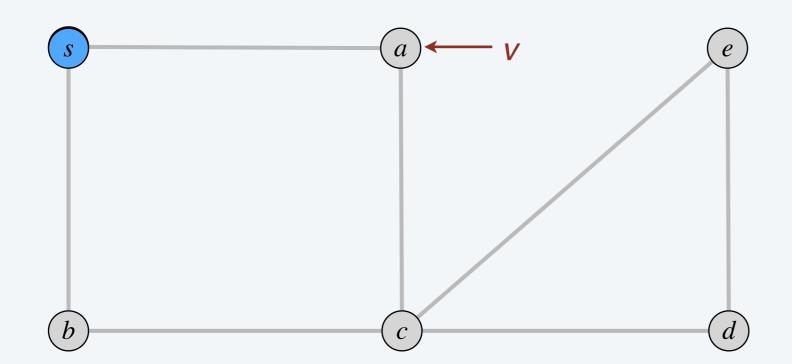
WHILE S is not empty

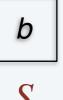
remove ("pop") the vertex v from the front of S

IF *v* is unexplored

mark v as explored

FOR each edge (v, w) in v's adjacency-list add ("push") w to the front of S





S

5

mark all vertices as unexplored

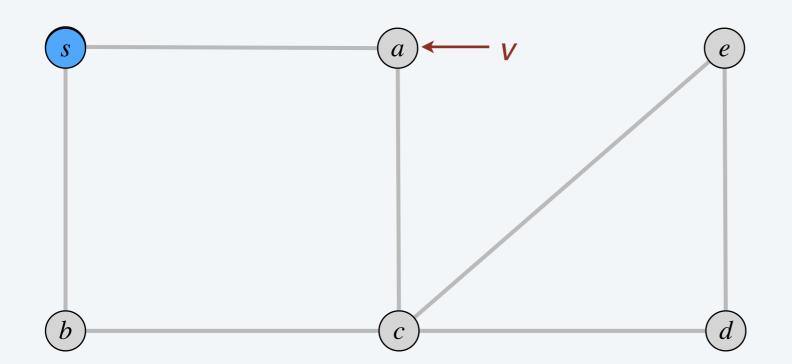
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mark v as explored





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 $S \leftarrow$ a stack data structure, initialized with s

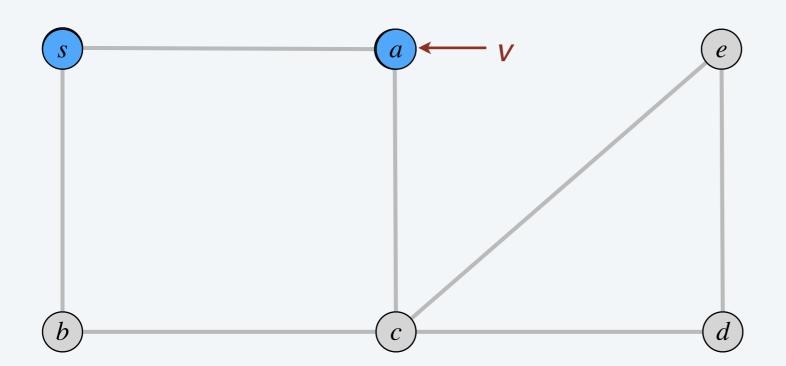
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S

2

mark all vertices as unexplored

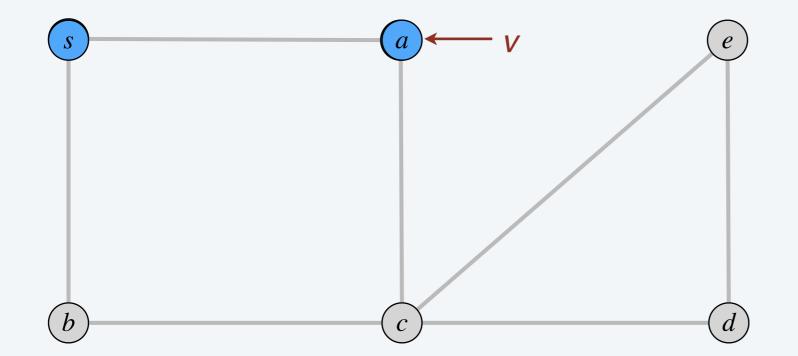
 $S \leftarrow$ a stack data structure, initialized with s

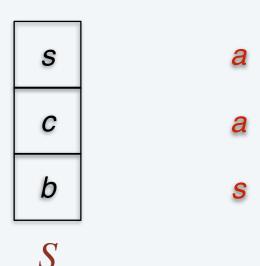
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mark all vertices as unexplored

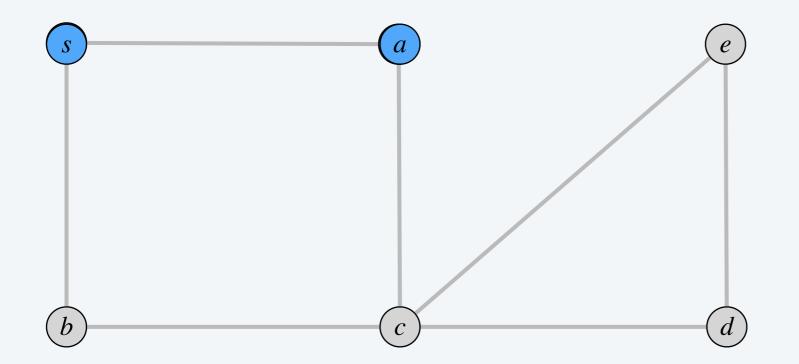
 $S \leftarrow$ a stack data structure, initialized with s

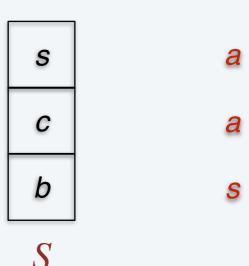
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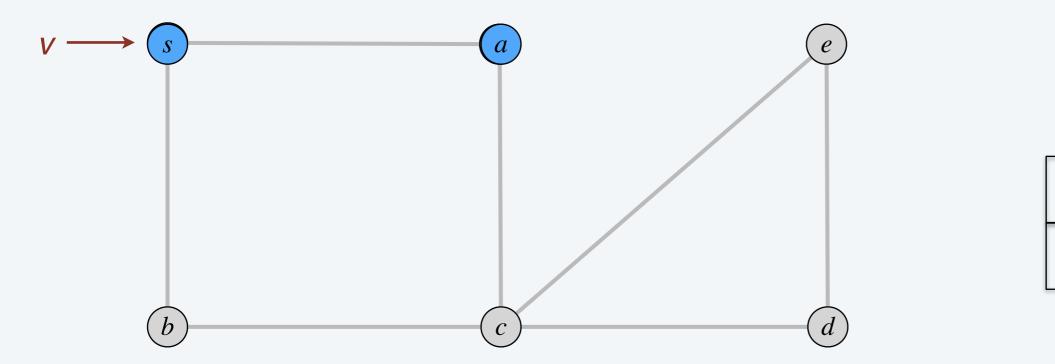
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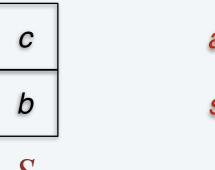
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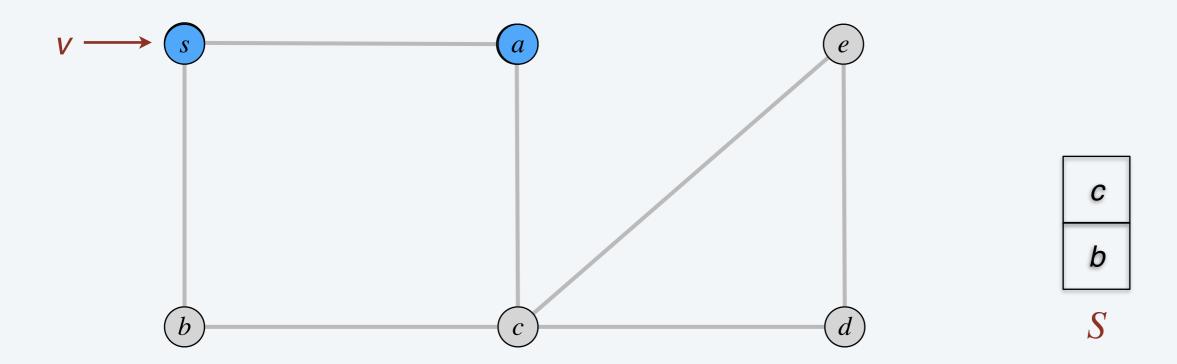
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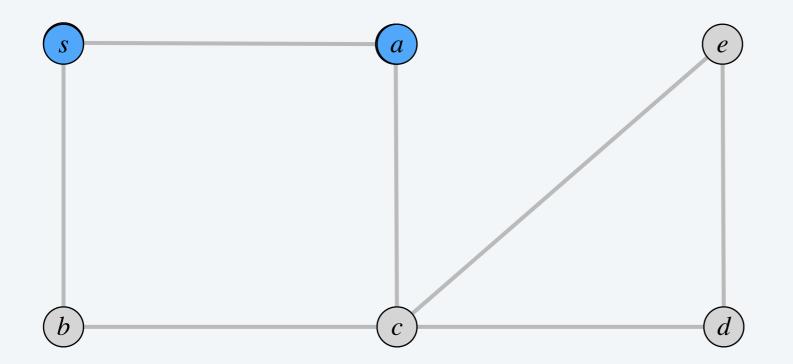
 $S \leftarrow$ a stack data structure, initialized with s

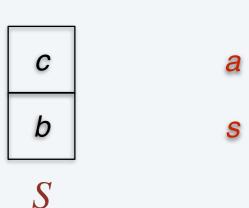
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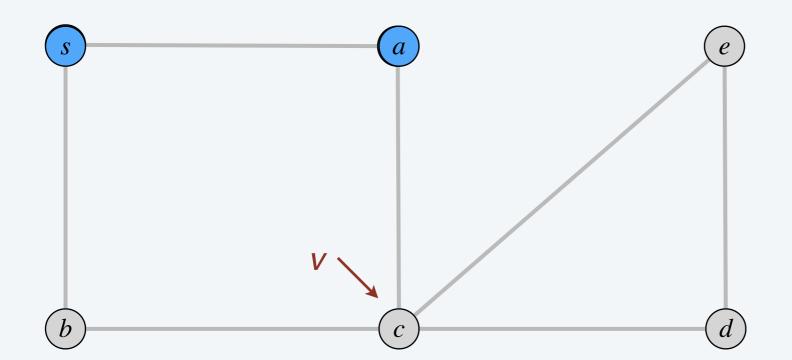
 $S \leftarrow$ a stack data structure, initialized with s

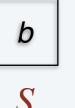
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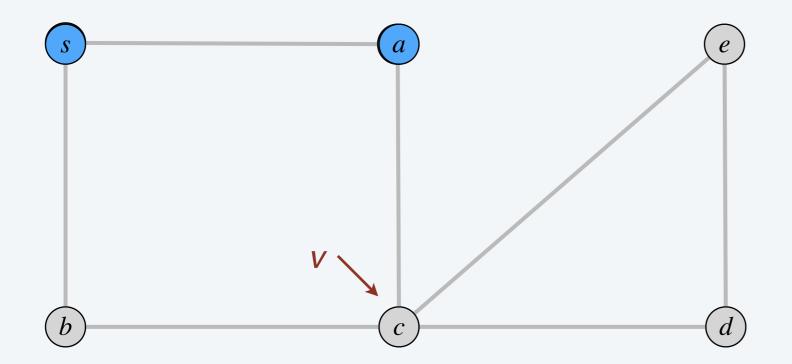
 $S \leftarrow$ a stack data structure, initialized with s

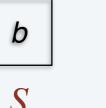
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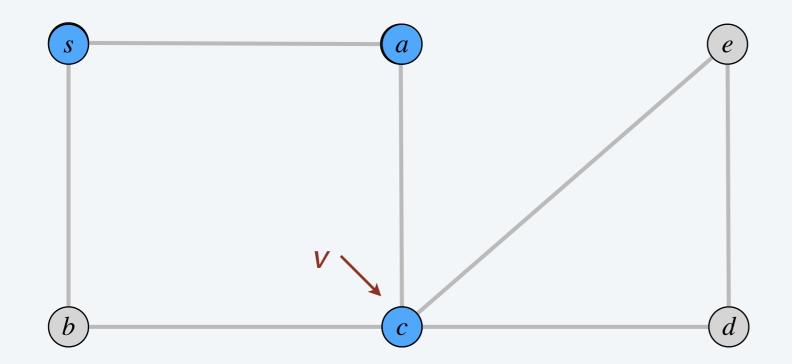
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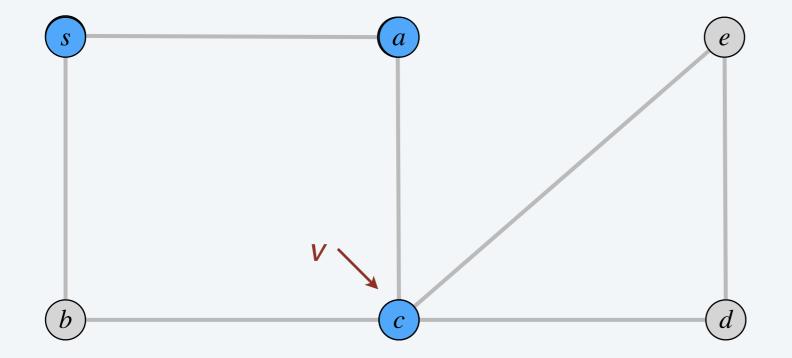
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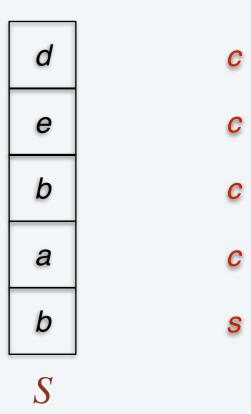
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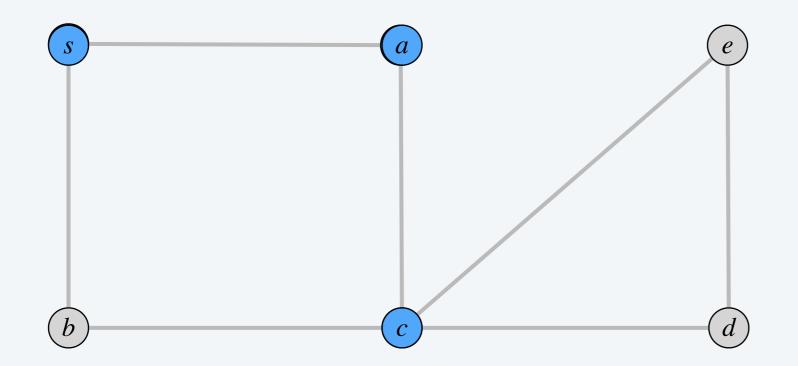
 $S \leftarrow$ a stack data structure, initialized with s

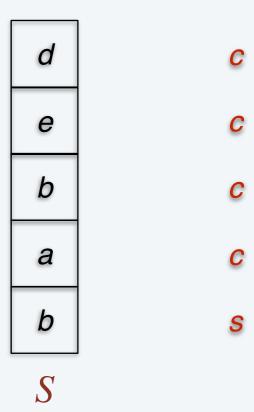
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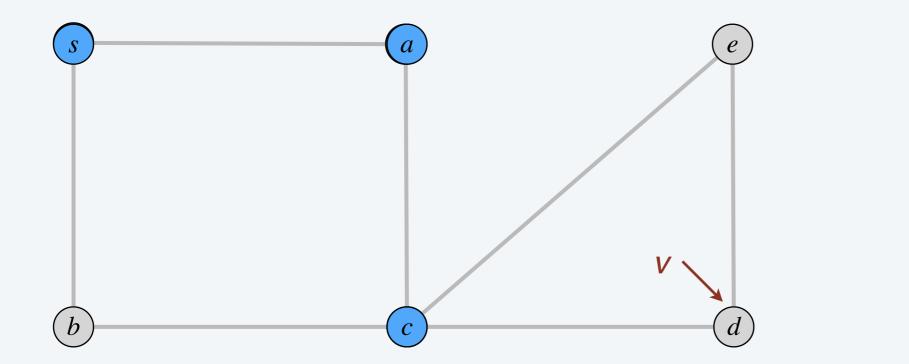
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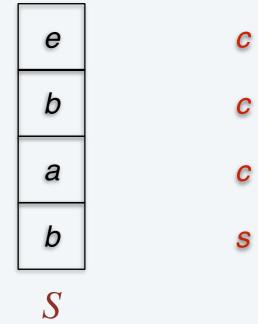
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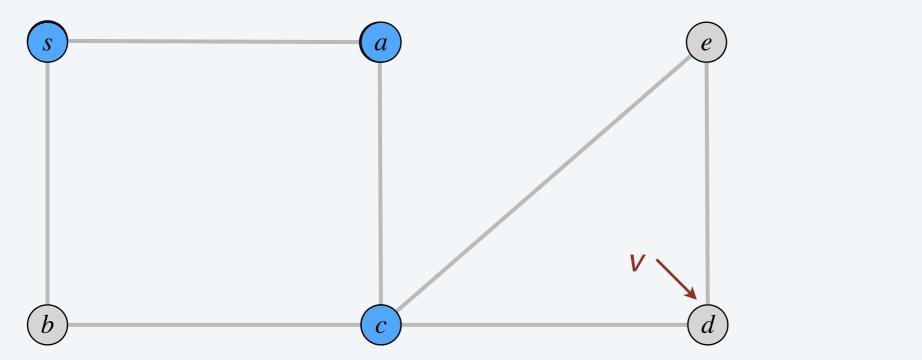
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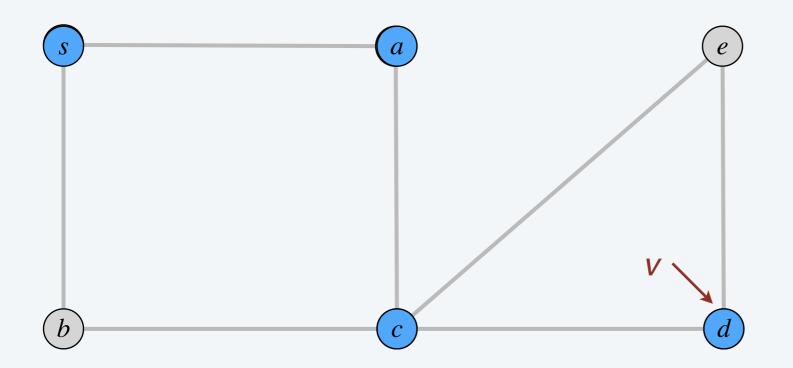
 $S \leftarrow$ a stack data structure, initialized with s

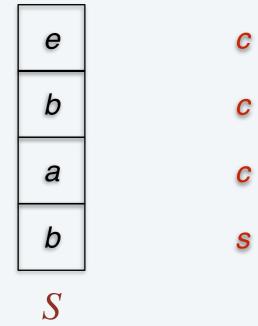
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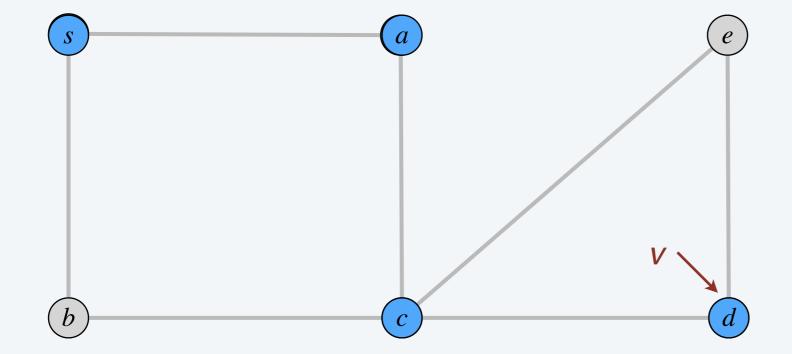
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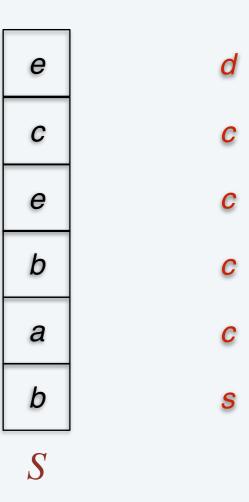
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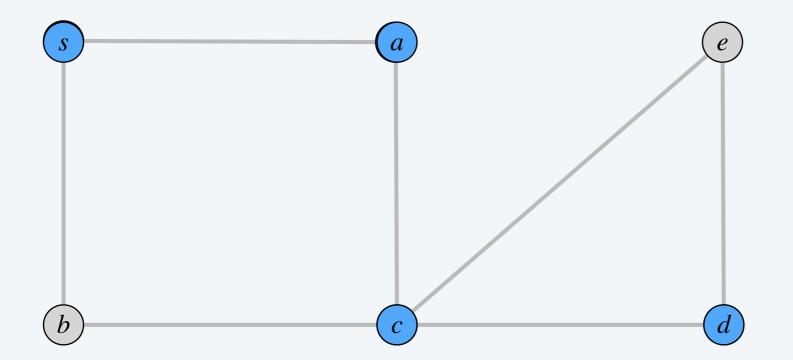
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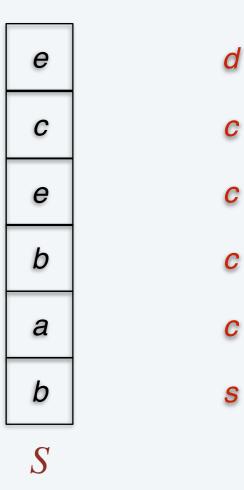
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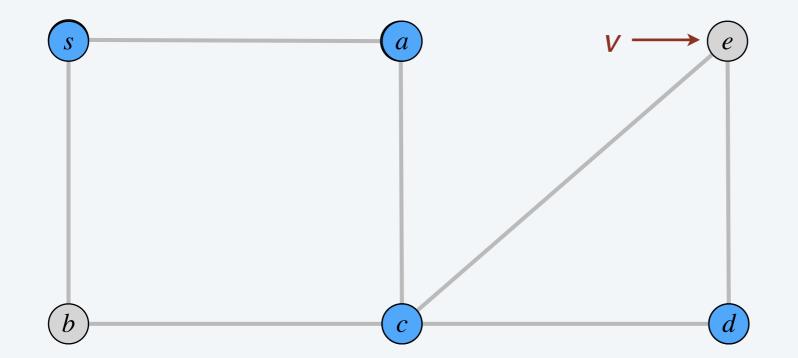
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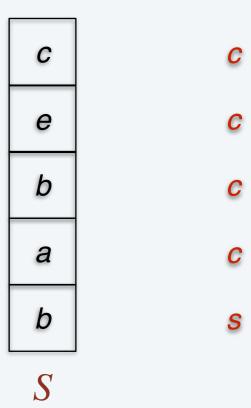
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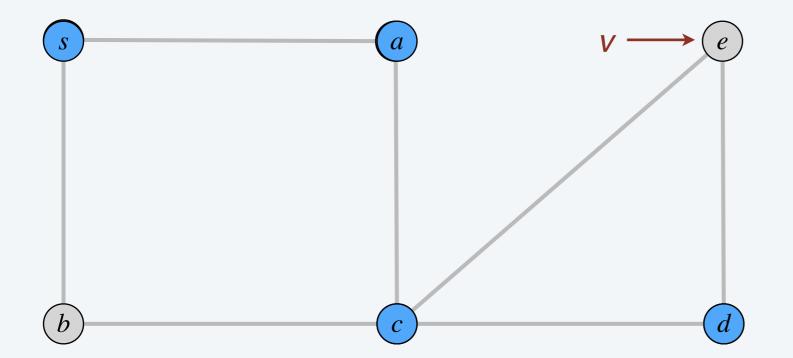
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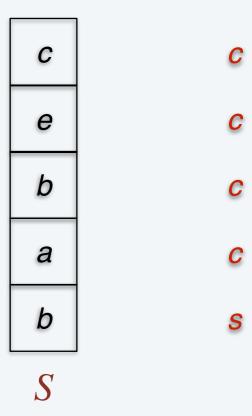
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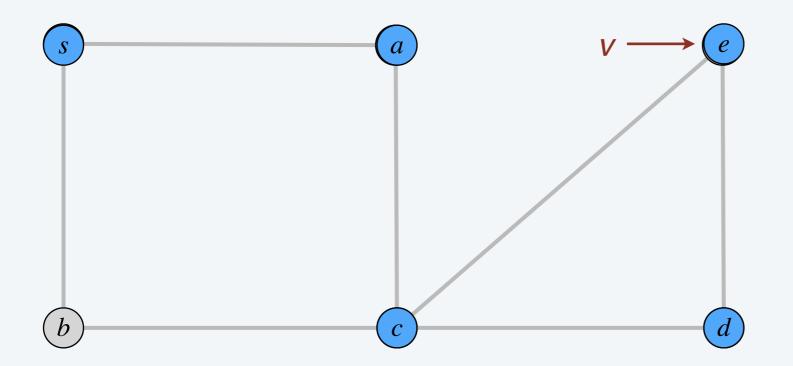
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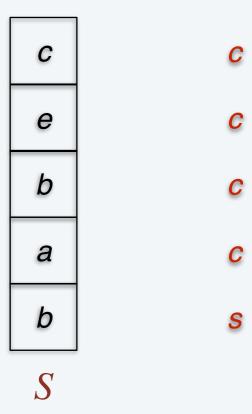
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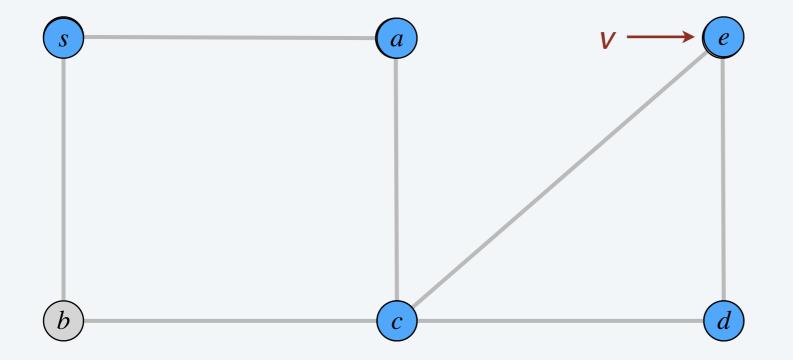
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	•
С	ϵ
d	ϵ
С	C
e	C
b	C
a	C
b	S
S	

mark all vertices as unexplored

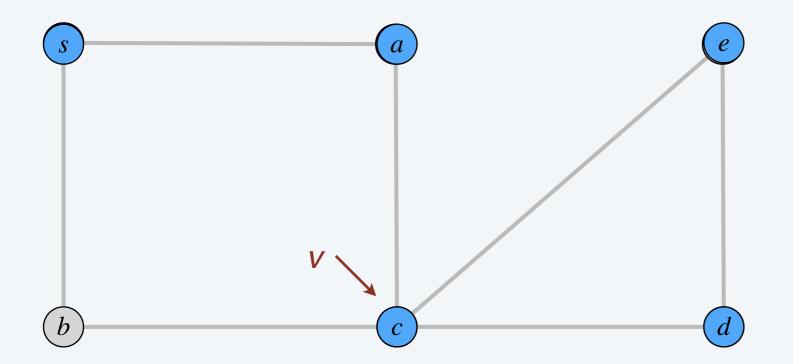
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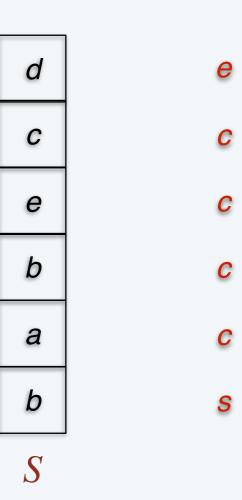
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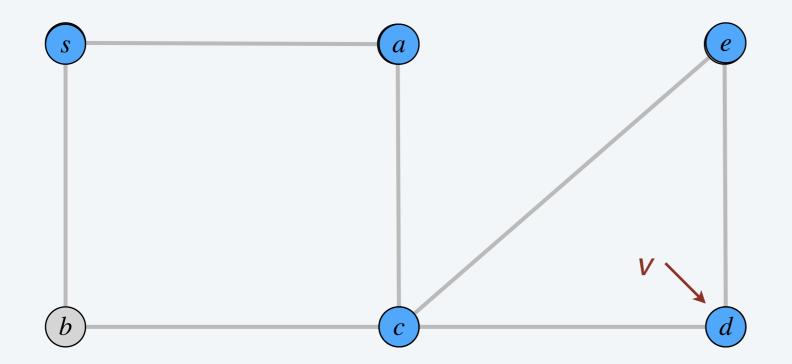
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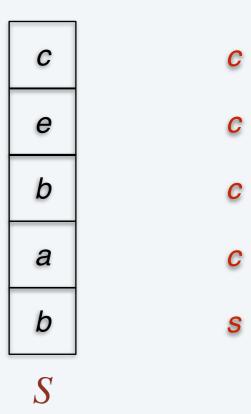
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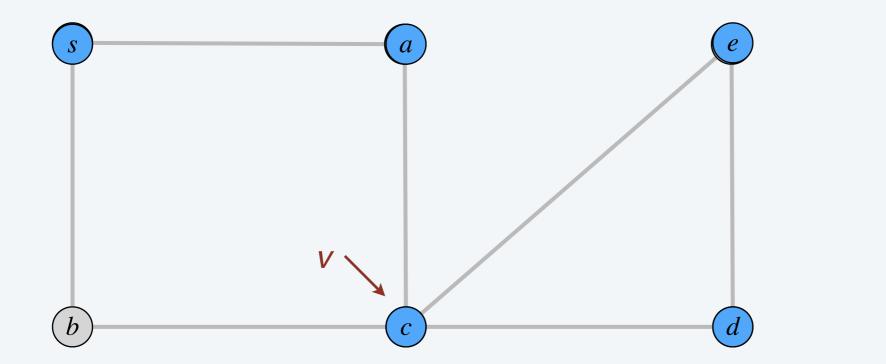
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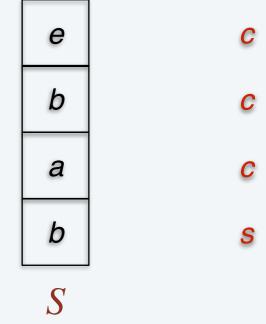
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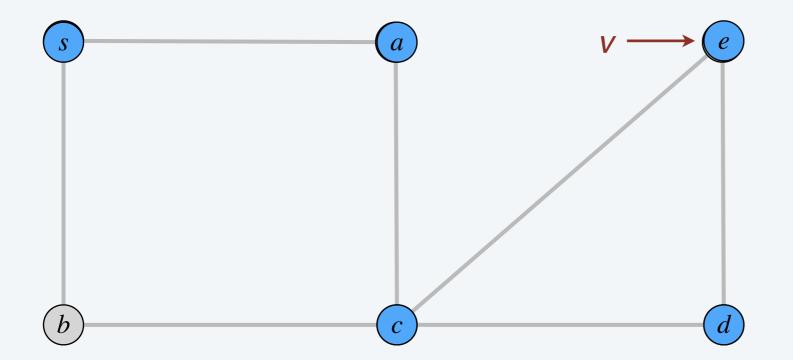
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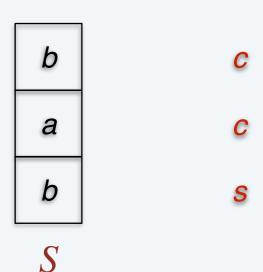
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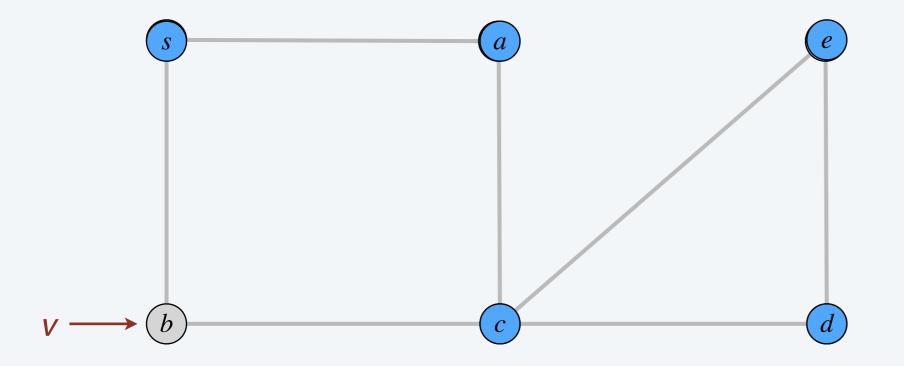
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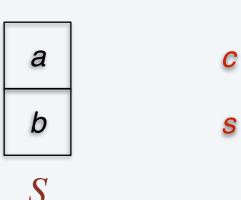
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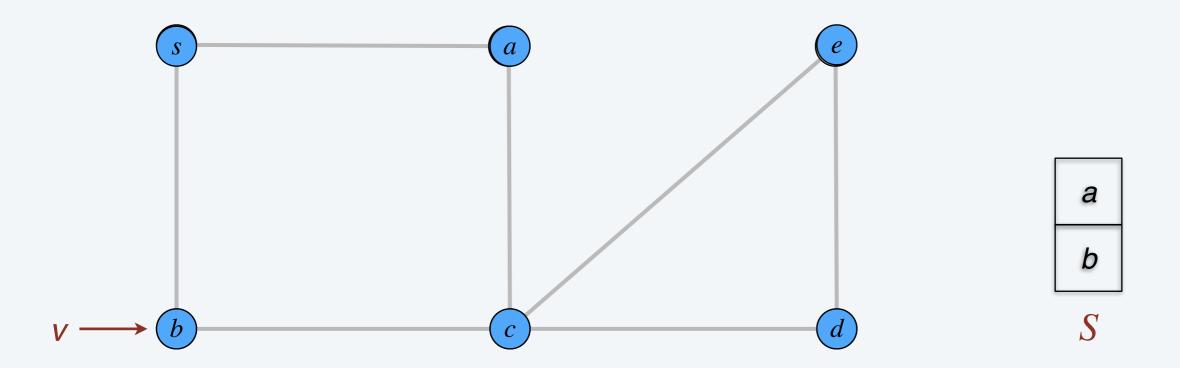
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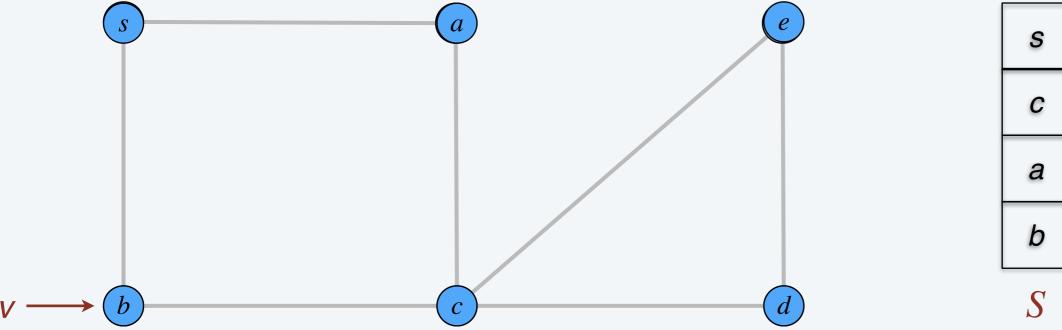
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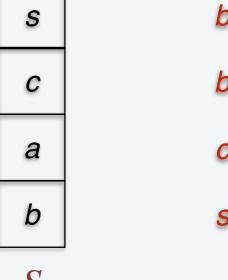
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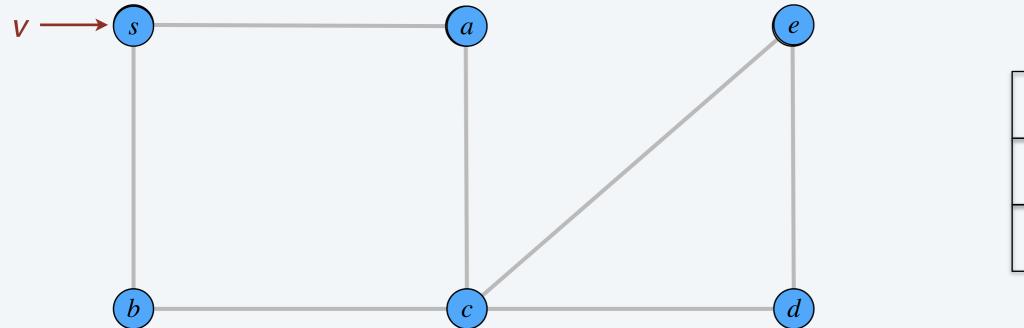
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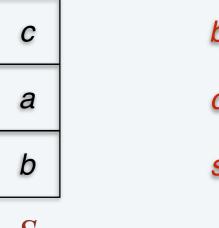
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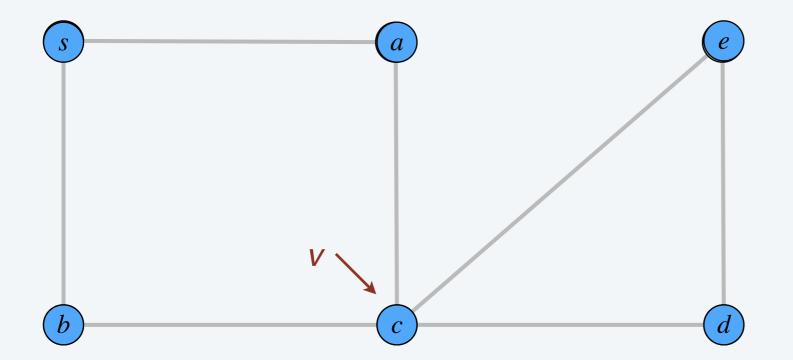
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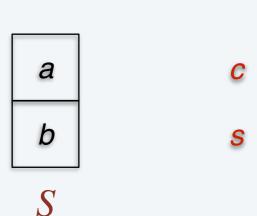
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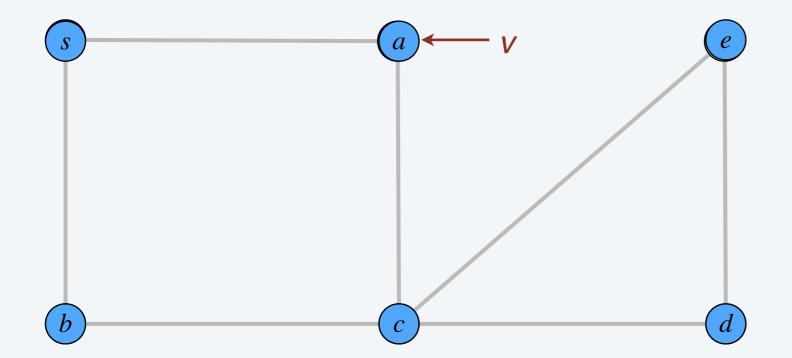
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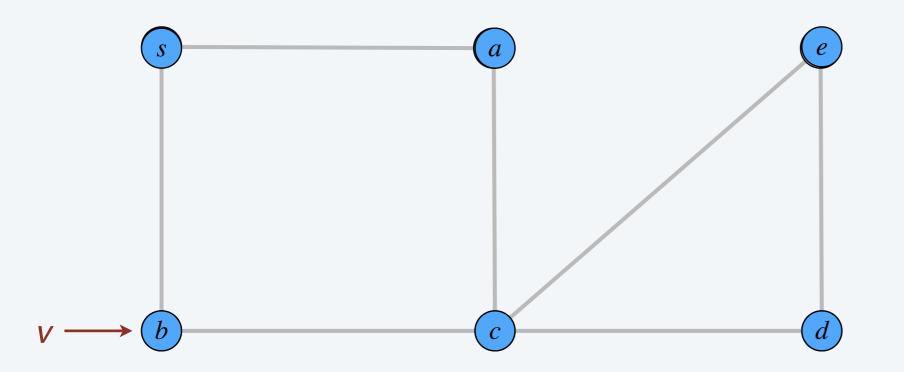
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